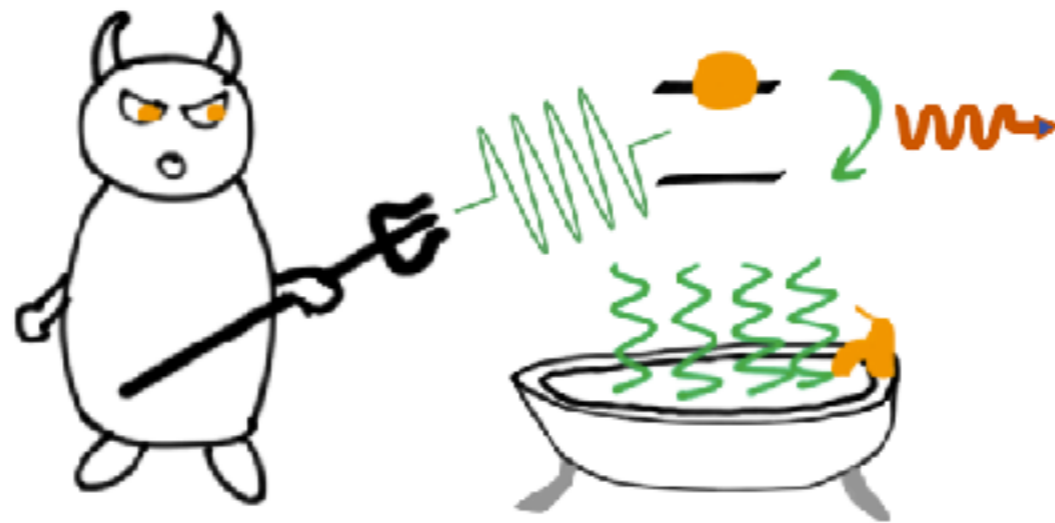


# Quantum thermodynamics of fluorescence and « quantum heat »

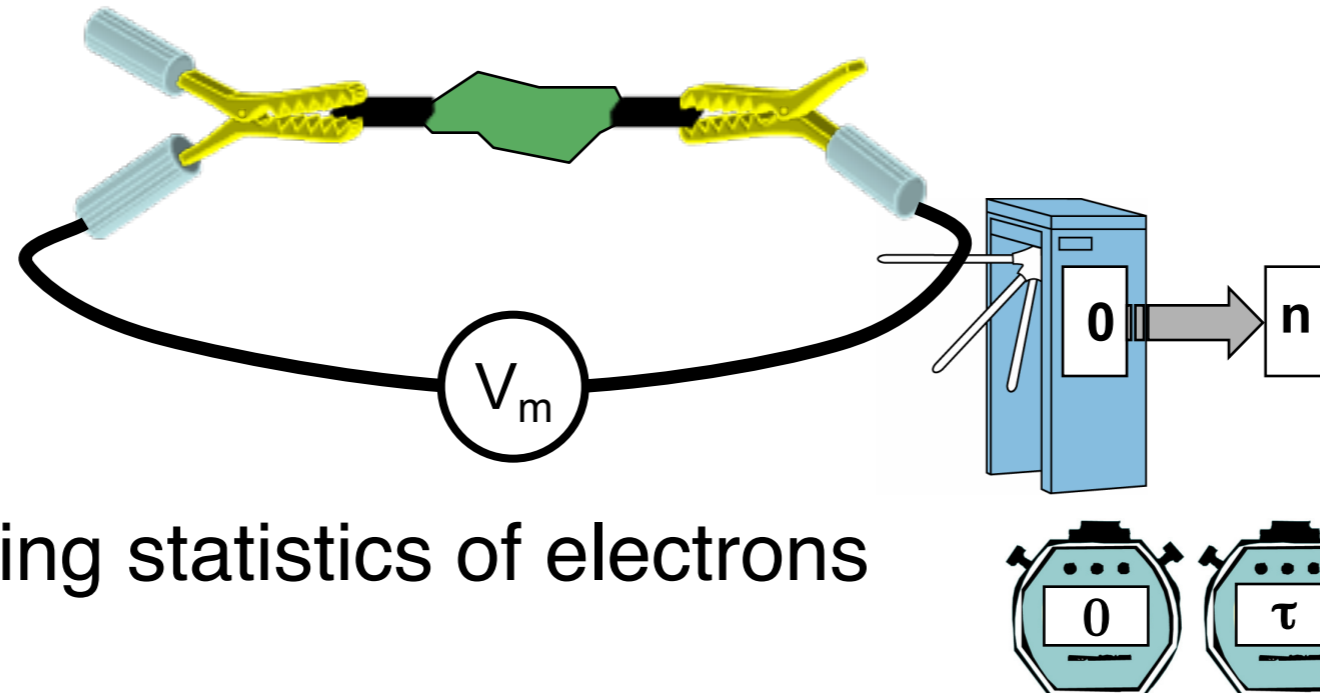
**Benjamin Huard**

Ecole Normale Supérieure de Lyon, France



Happy birthday Jukka!

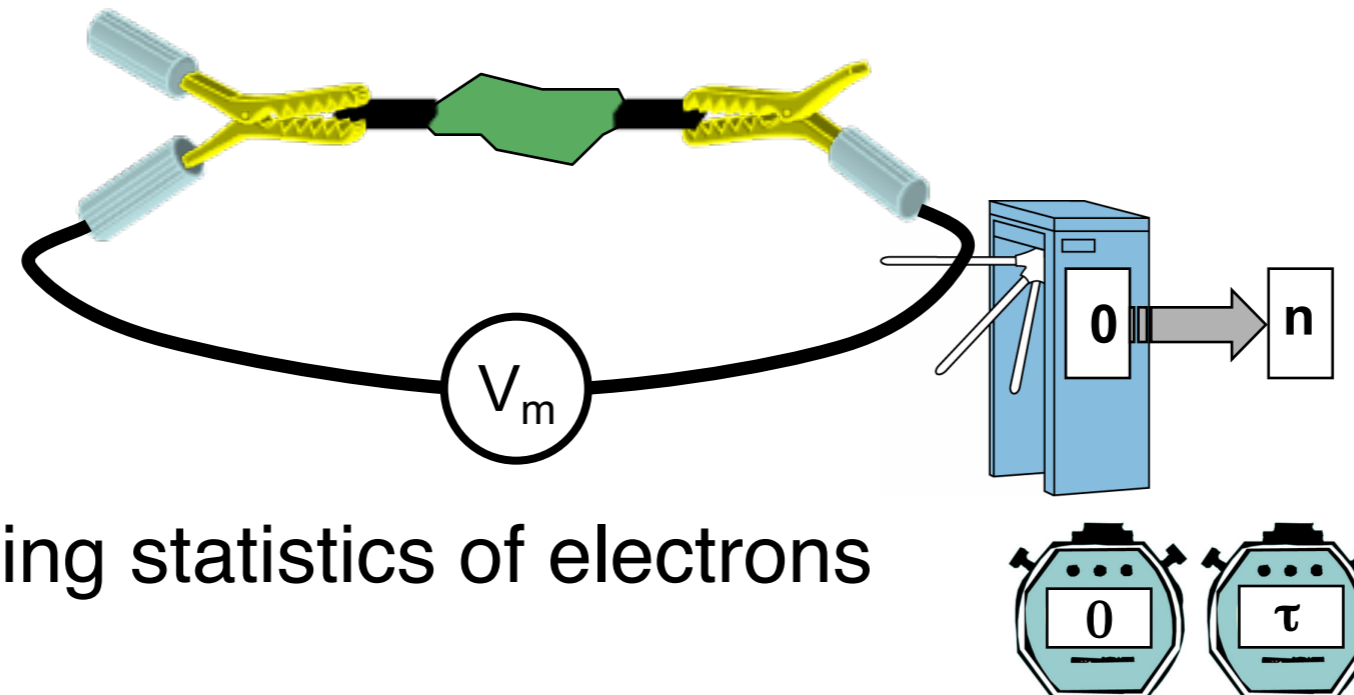
2004-2007



Full counting statistics of electrons

[Levitov, Lesovik, JETP 1993]

2004-2007



Full counting statistics of electrons

PRL 98, 207001 (2007)

PHYSICAL REVIEW LETTERS

week ending  
18 MAY 2007

## Wideband Detection of the Third Moment of Shot Noise by a Hysteretic Josephson Junction

A. V. Timofeev,<sup>1,2</sup> M. Meschke,<sup>1</sup> J. T. Peltonen,<sup>1</sup> T. T. Heikkilä,<sup>1</sup> and J. P. Pekola<sup>1</sup>

<sup>1</sup>*Low Temperature Laboratory, Helsinki University of Technology, P.O. Box 3500, 02015 TKK, Finland*

<sup>2</sup>*Institute of Solid State Physics, Russian Academy of Sciences, Chernogolovka, 142432 Russia*

(Received 4 December 2006; published 16 May 2007)

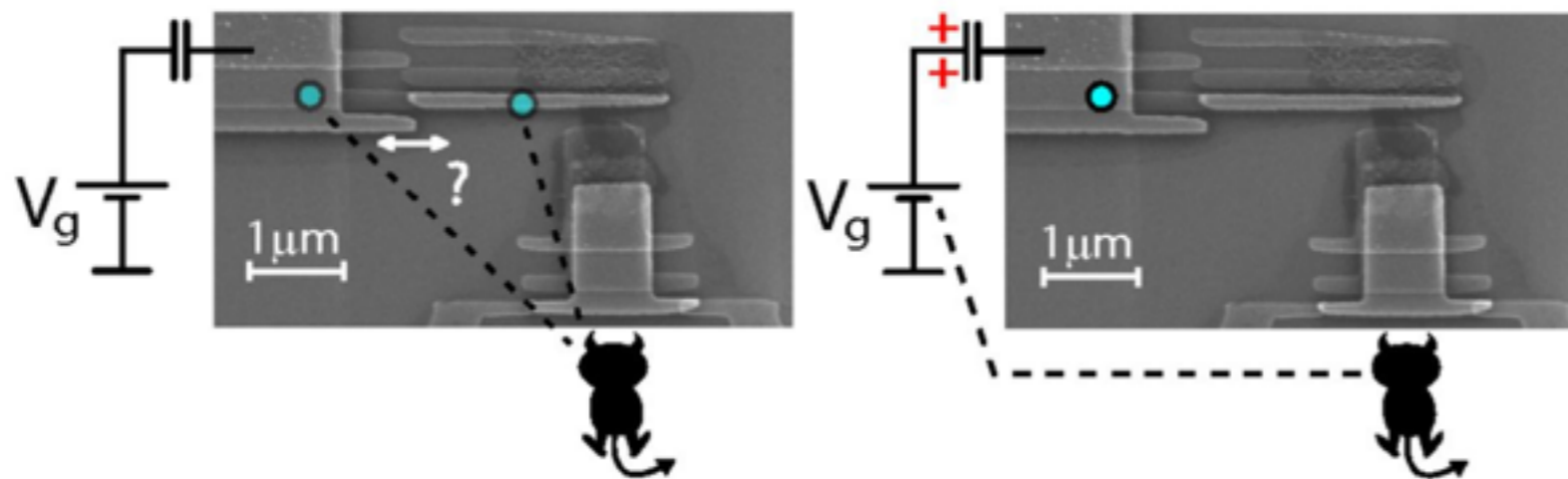
Ann. Phys. (Leipzig) 16, No. 10–11, 736–750 (2007) / DOI 10.1002/andp.200710263

## Josephson junctions as detectors for non-Gaussian noise

B. Huard<sup>1,\*</sup>, H. Pothier<sup>1,\*\*</sup>, Norman O. Birge<sup>1,\*\*\*</sup>, D. Esteve<sup>1</sup>, X. Waintal<sup>2</sup>, and J. Ankerhold<sup>3</sup>

new common interest

## Thermodynamics with mesoscopic circuits



[J. Koski, V. Maisi, J. Pekola, D. Averin, PNAS 2014]

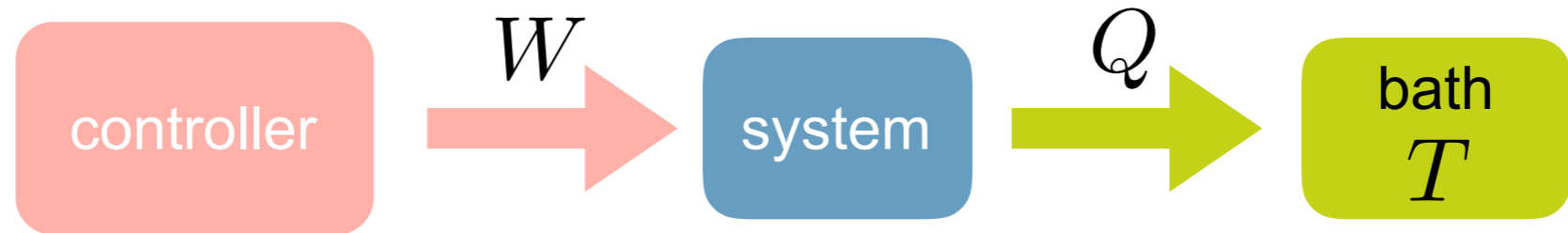


Quantum Thermodynamics Conference  
QTD2019

Right here next June!

# Quantum measurement thermodynamics

Thermodynamics with thermal baths



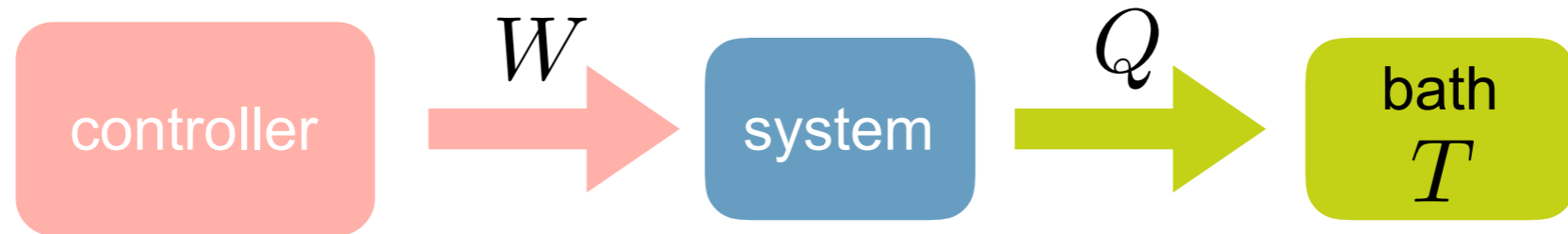
thermal noise

$$U(t) \equiv \langle H_{\text{sys}} \rangle_{\rho(t)}$$

$$U(t) - U(0) = W - Q \quad \text{1st law}$$

# Quantum measurement thermodynamics

## Thermodynamics with thermal baths

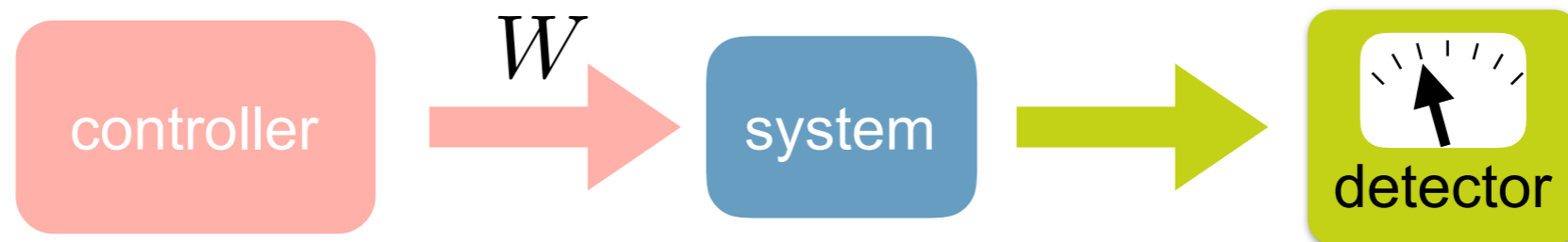


thermal noise

$$U(t) \equiv \langle H_{\text{sys}} \rangle_{\rho(t)}$$

$$U(t) - U(0) = W - Q \quad \text{1st law}$$

## Thermodynamics with quantum measurements (no thermal bath required)

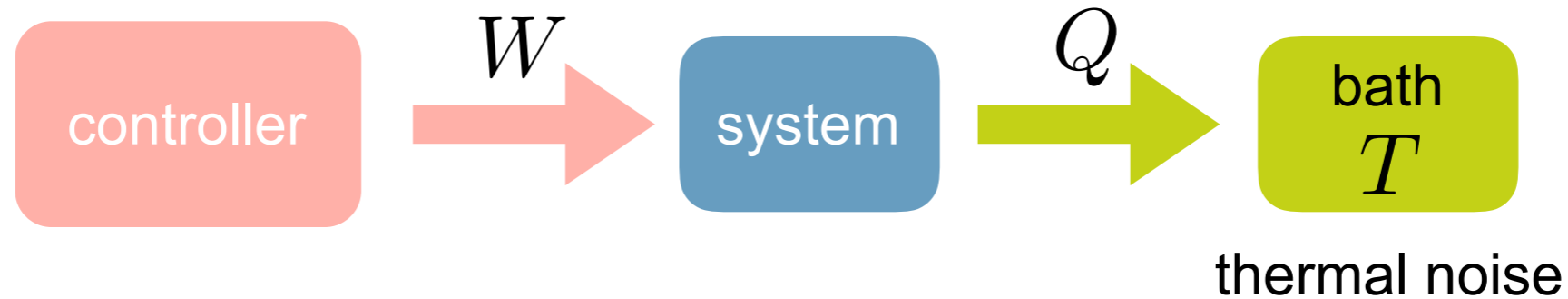


random outcomes

$$U(t) - U(0) \neq W \quad \text{the system energy can vary by measurement backaction}$$

# Quantum measurement thermodynamics

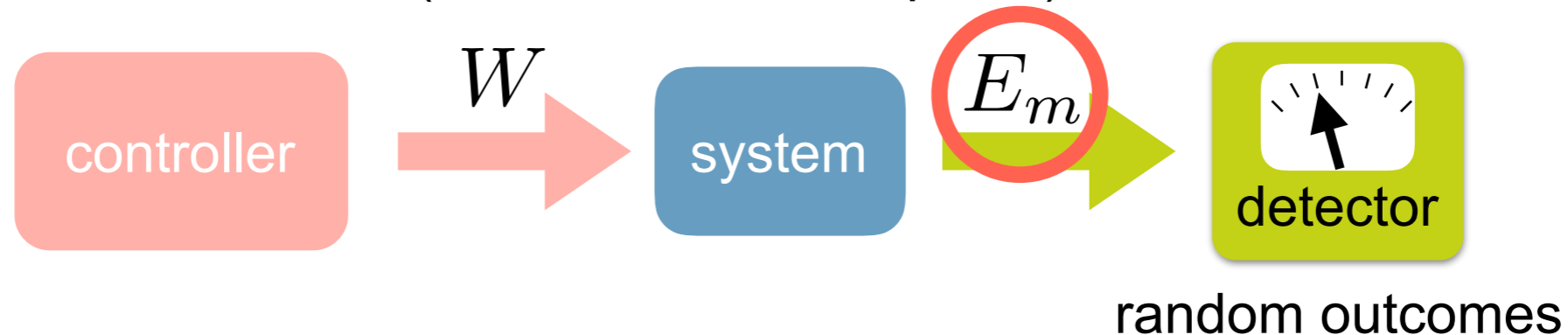
## Thermodynamics with thermal baths



$$U(t) \equiv \langle H_{\text{sys}} \rangle_{\rho(t)}$$

$$U(t) - U(0) = W - Q \quad \text{1st law}$$

## Thermodynamics with quantum measurements (no thermal bath required)



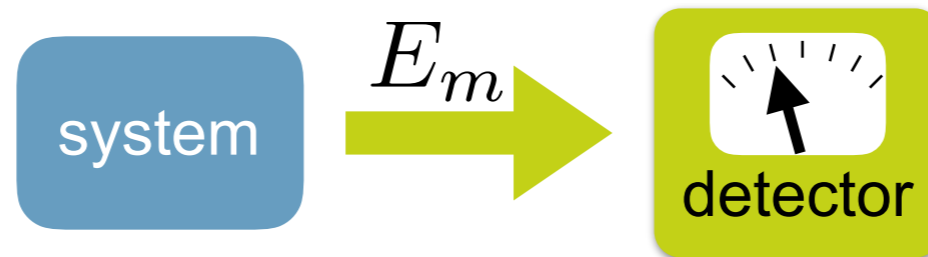
$U(t) - U(0) \neq W$  the system energy can vary by measurement backaction

$$\delta W = \text{Tr}(\rho dH) \quad \delta E_m = \text{Tr}(H d\rho)$$

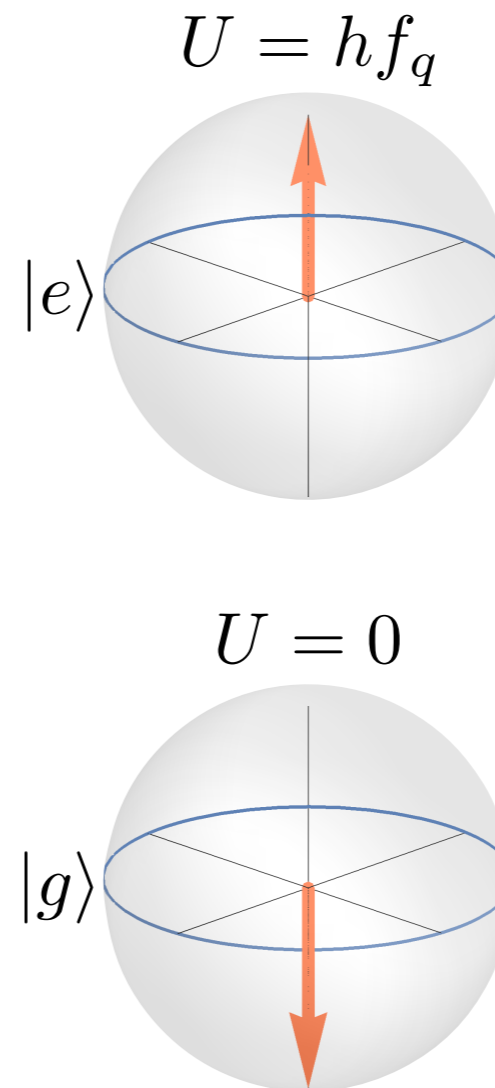
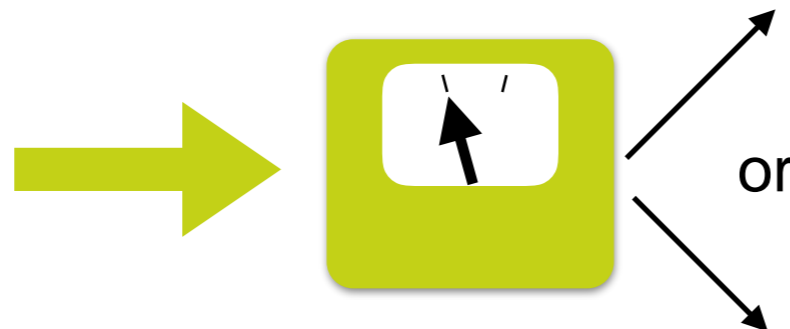
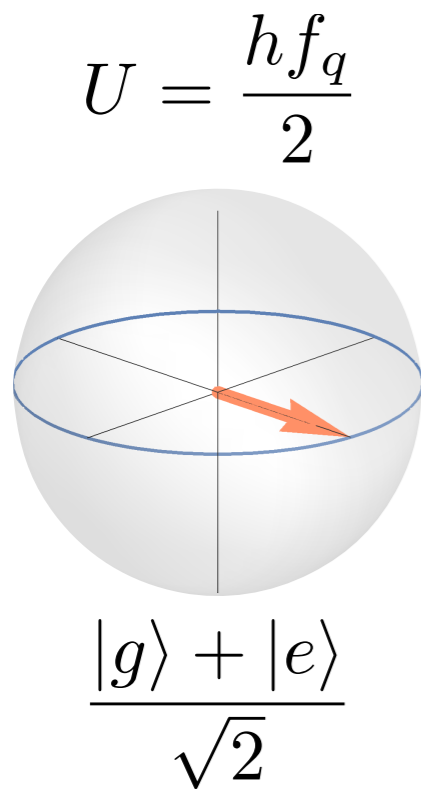
random energy change  $E_m$  because outcomes are stochastic  $\longrightarrow$  « quantum heat »

# « quantum heat »

« quantum heat »



simple example on a qubit



$$E_m = +\frac{hf_q}{2}$$

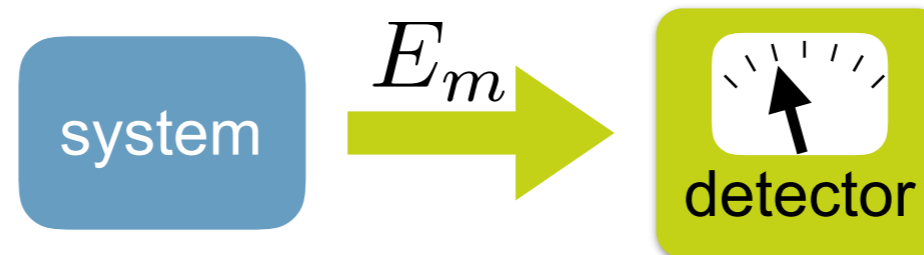
or

$$E_m = -\frac{hf_q}{2}$$



# « quantum heat »

« quantum heat »



**does it obey a second law?**

**yes**, fluctuation theorems can be extended with this work and « heat »

[Manzano, Horowitz and Parrondo, PRE 2015] [Alonso, Lutz and Romito, PRL (2016)]  
[Elouard, Auffèves and Clusel, npj QI (2017)] [Naghiloo et al., PRL (2018)] [Manikandan, Elouard, Jordan, arxiv 2018]

**can it fuel an engine?**

**yes**, repeatedly measuring  $\sigma_x$  on a qubit can provide work on a cycle

[Yi, Talkner, Kim, PRE 2017] [Elouard, Herrera-Martí, Huard, Auffèves, PRL (2017)]  
[Elouard, Jordan, PRL (2018)] [Ding, Yi, Kim, Talkner, arxiv 2018] [Buffoni et al., arxiv 2018]

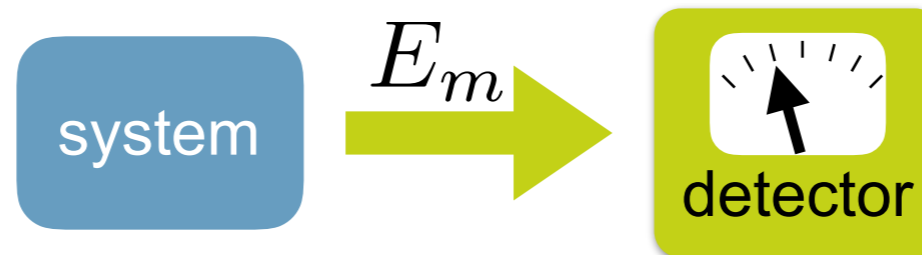
Michele's talk

**what provides this energy?**

**can it be measured directly and not just inferred?**

# « quantum heat »

« quantum heat »



**does it obey a second law?**

**yes**, fluctuation theorems can be extended with this work and « heat »

[Manzano, Horowitz and Parrondo, PRE 2015] [Alonso, Lutz and Romito, PRL (2016)]  
[Elouard, Auffèves and Clusel, npj QI (2017)] [Naghiloo et al., PRL (2018)] [Manikandan, Elouard, Jordan, arxiv 2018]

**can it fuel an engine?**

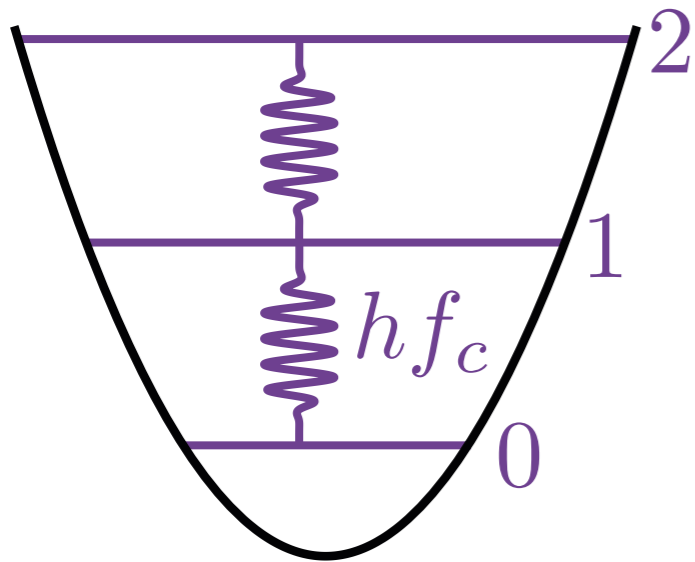
**yes**, repeatedly measuring  $\sigma_x$  on a qubit can provide work on a cycle

[Yi, Talkner, Kim, PRE 2017] [Elouard, Herrera-Martí, Huard, Auffèves, PRL (2017)]  
[Elouard, Jordan, PRL (2018)] [Buffoni et al., arxiv 2018] [Ding, Yi, Kim, Talkner, arxiv 2018]

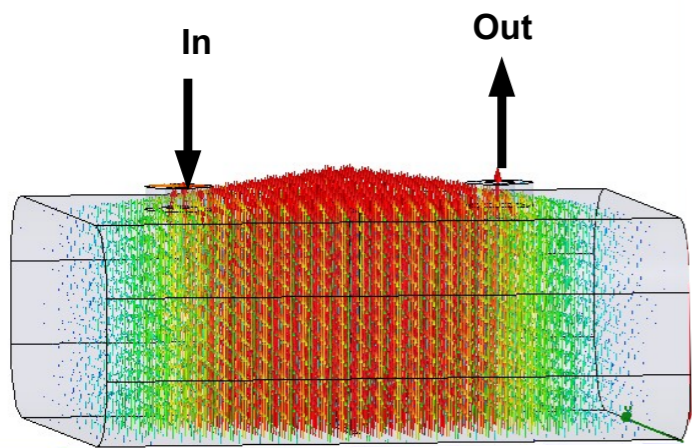
**what provides this energy?**

**can it be measured directly and not just inferred?**

# 3D transmon



$$H_c = hf_c \left( a^\dagger a + \frac{1}{2} \right)$$



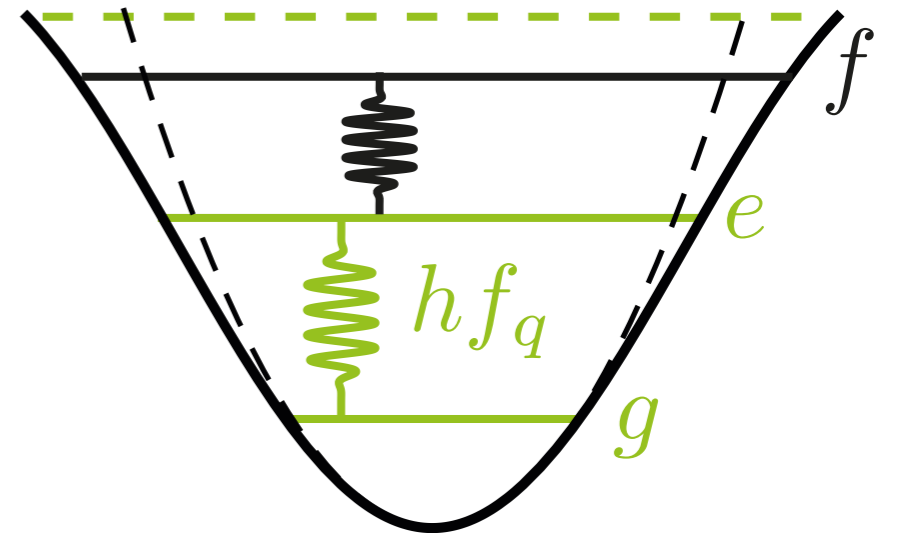
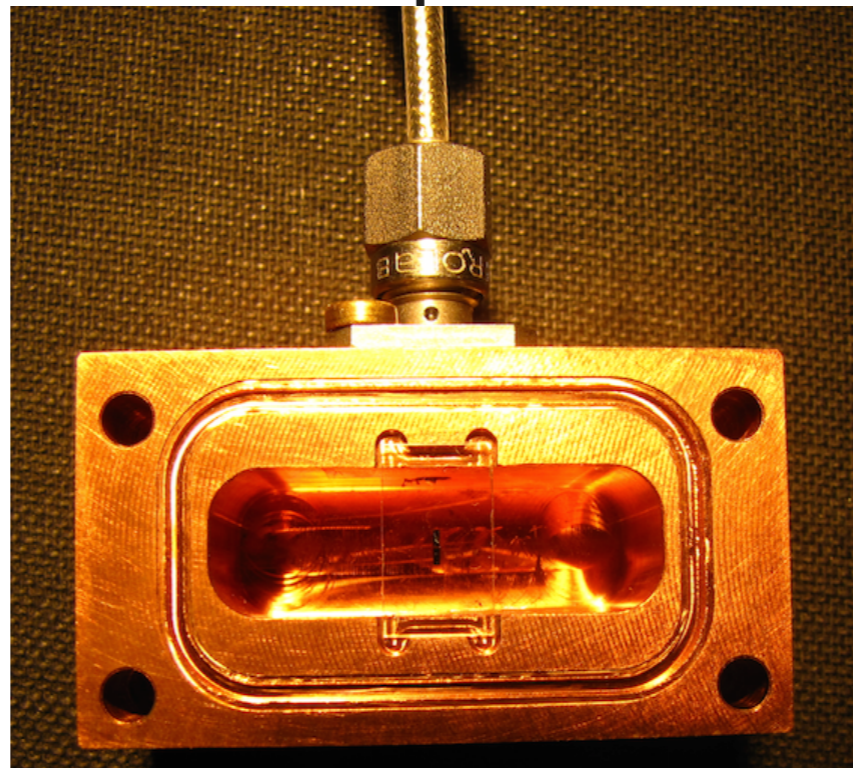
$$f_c = 7.5 \text{ GHz}$$

$$kT \ll hf$$

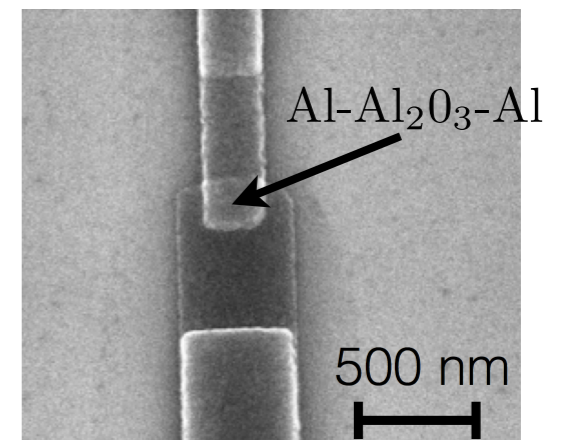
$$T = 20 \text{ mK}$$

$$H_{\text{disp}} = h\chi \frac{\sigma_z}{2} a^\dagger a$$

$$\chi = 9.6 \text{ MHz}$$



$$H_q = \frac{hf_q}{2} \sigma_z$$

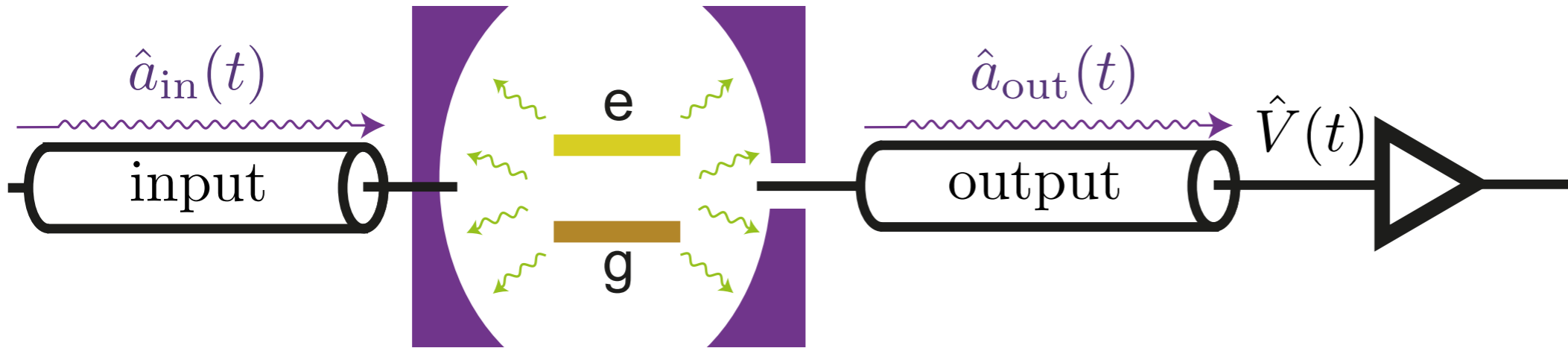


$$\text{In cavity, } f_q = 6.3 \text{ GHz}$$

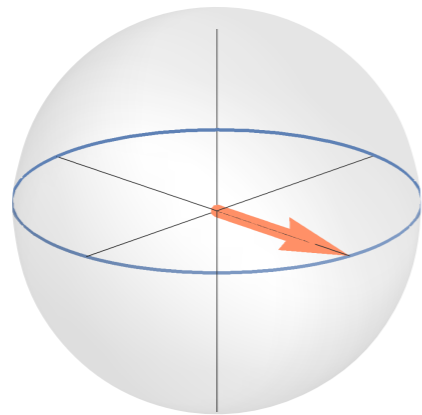
$$\gamma_1 = (4.2 \mu\text{s})^{-1}$$

# Dispersive Measurement

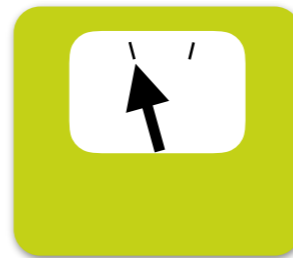
$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



$$U = \frac{hf_q}{2}$$

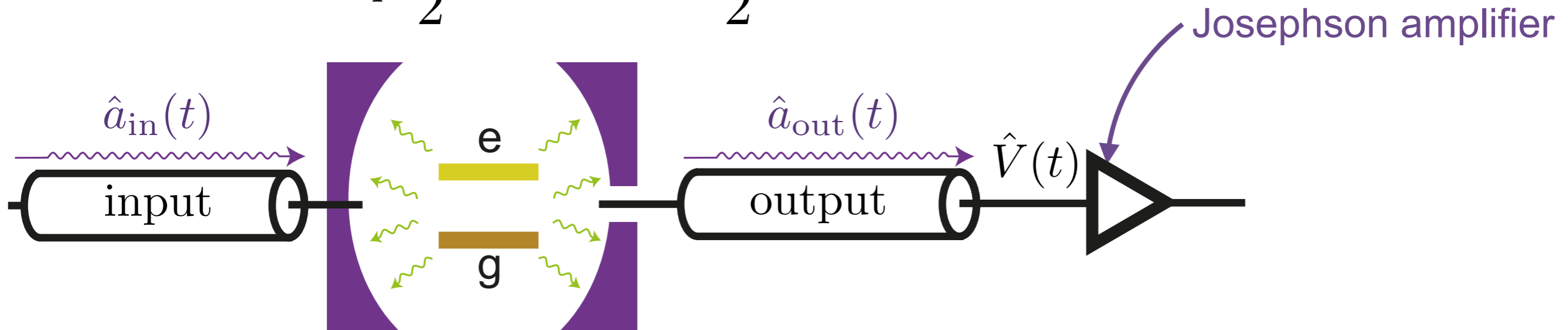


$$\frac{|g\rangle + |e\rangle}{\sqrt{2}}$$



# Dispersive Measurement

$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



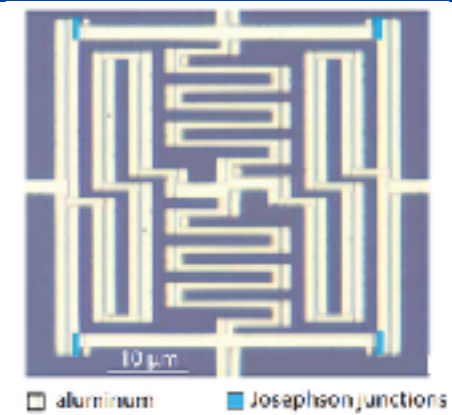
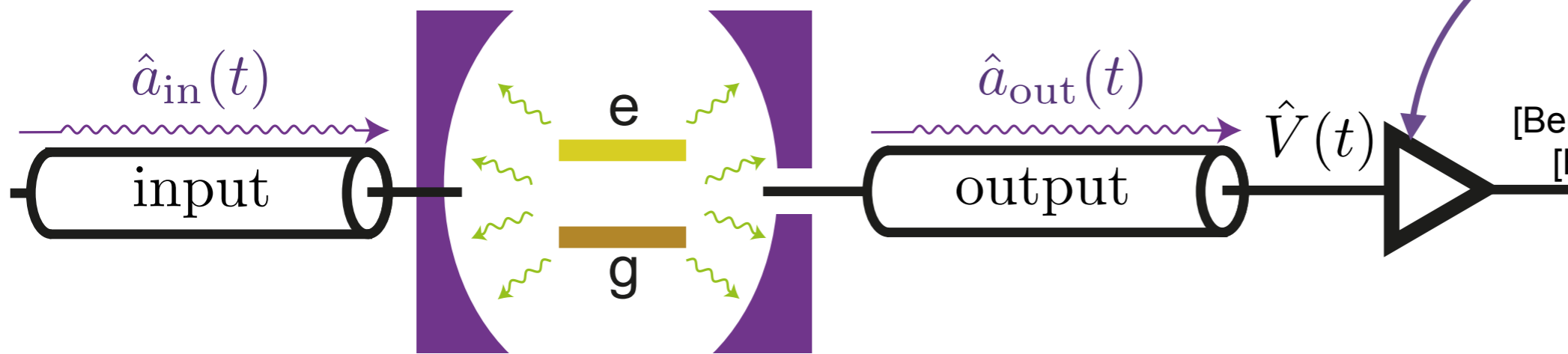
Classically  $V(t) = I(t) \cos(2\pi f_c t) + Q(t) \sin(2\pi f_c t)$

$$I_t \rightarrow \hat{I}_t \propto \frac{\hat{a}_{out} + \hat{a}_{out}^\dagger}{2} = \text{Re}(\hat{a}_{out})$$

$$Q_t \rightarrow \hat{Q}_t \propto \frac{\hat{a}_{out} - \hat{a}_{out}^\dagger}{2i} = \text{Im}(\hat{a}_{out})$$

# Dispersive Measurement

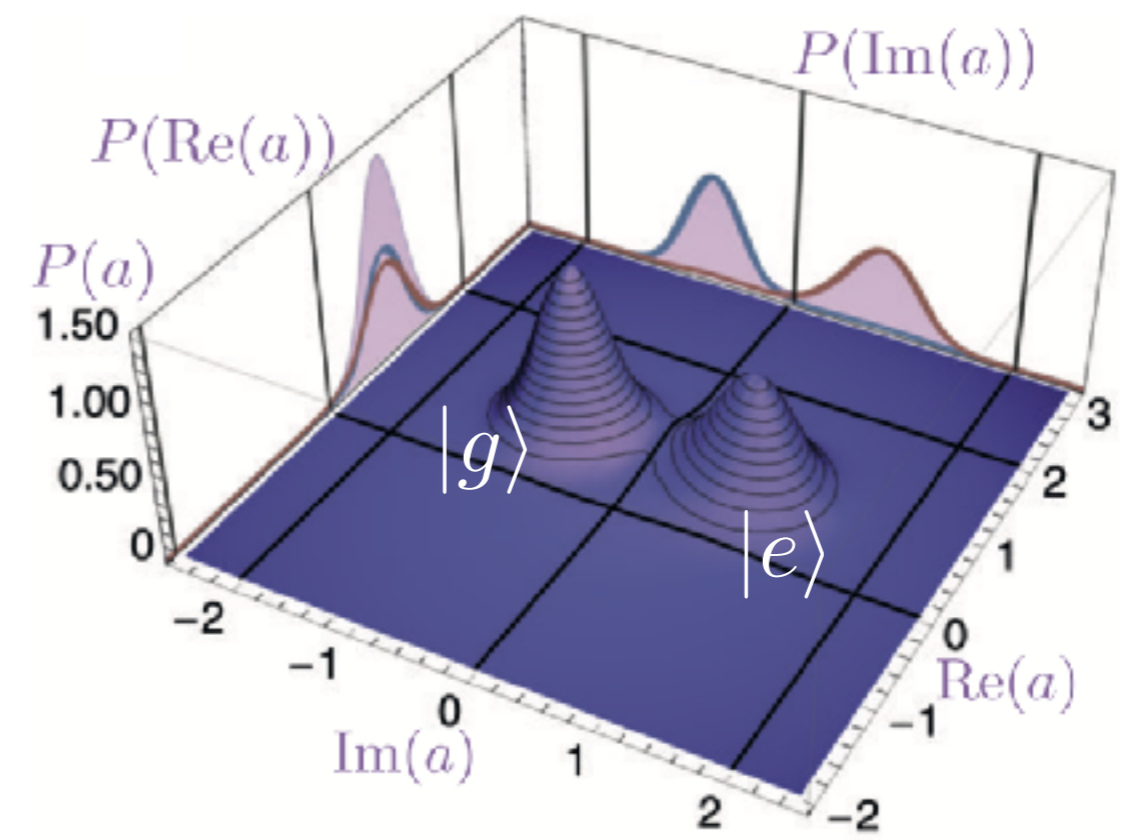
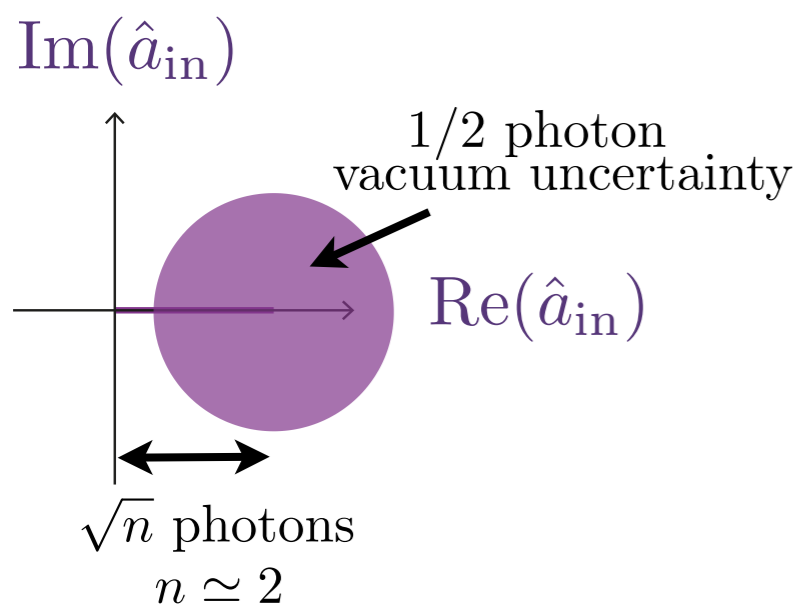
$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



[Bergeal *et al.*, Nature 2010]  
[Roch *et al.*, PRL 2012]

... field coming out

field going in ...

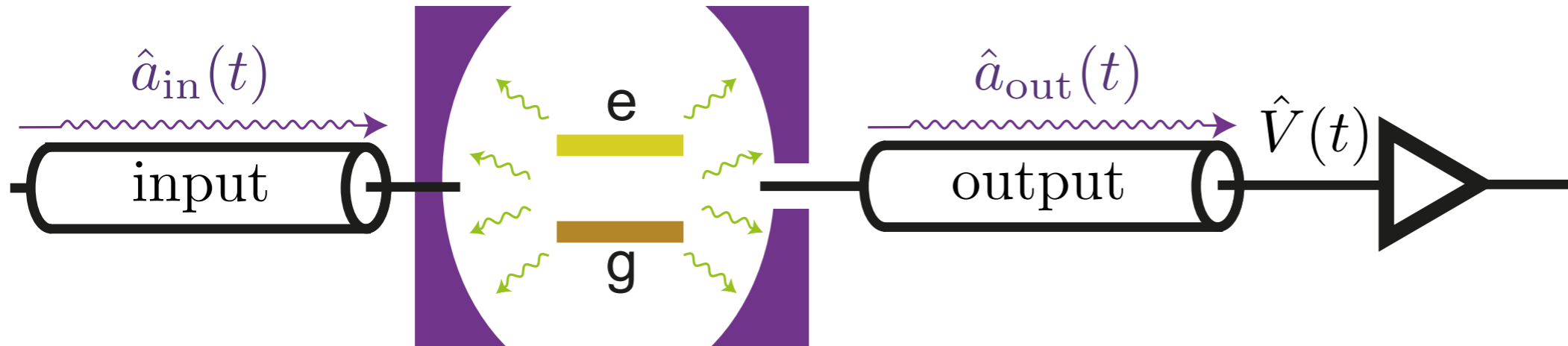


the phase changes depending on qubit state

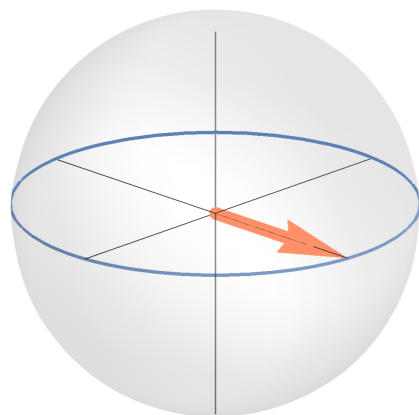
[Campagne-Ibarcq *et al.*, PRX 2013]

# Dispersive Measurement

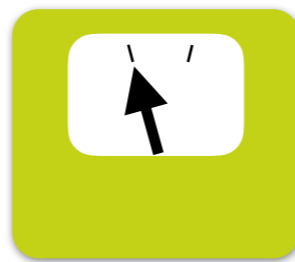
$$H = hf_q \frac{\sigma_z}{2} + h(f_c - \frac{\chi}{2} \sigma_z) a^\dagger a$$



$$U = \frac{hf_q}{2}$$



$$\frac{|g\rangle + |e\rangle}{\sqrt{2}}$$



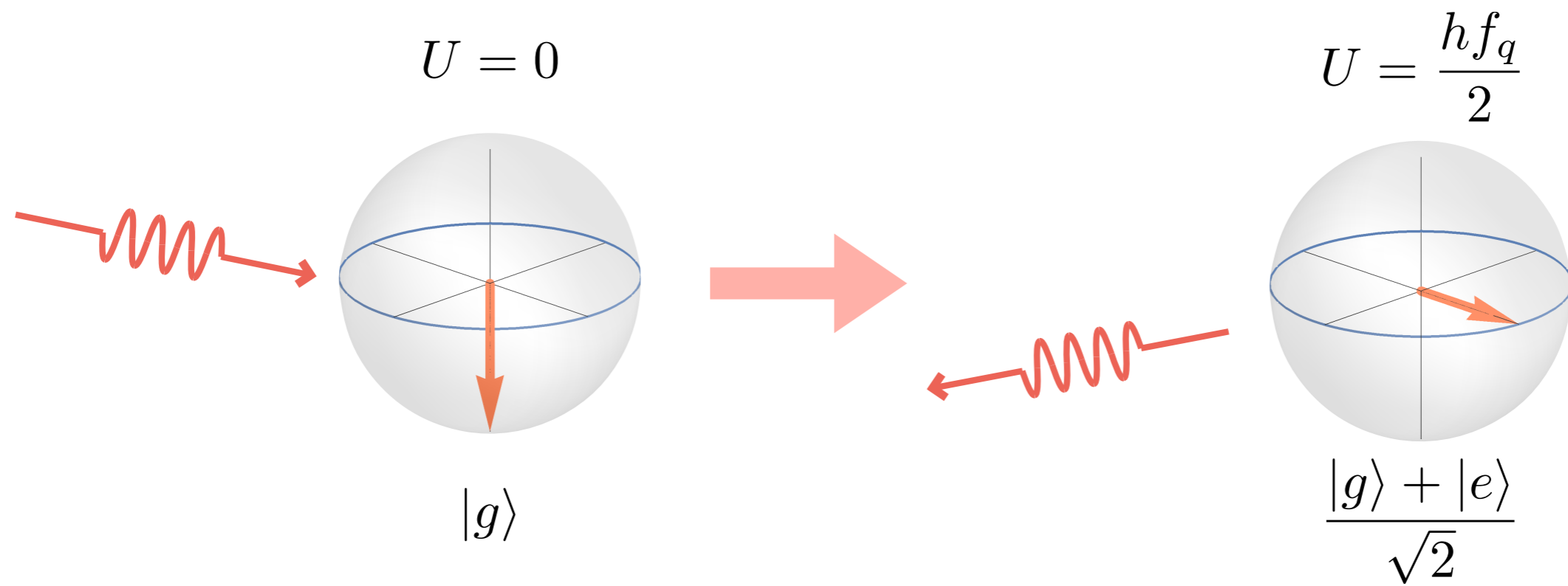
only the phase changes  
not the field **amplitude**

no matter what the qubit state is,

$$P_{in} = P_{out}$$

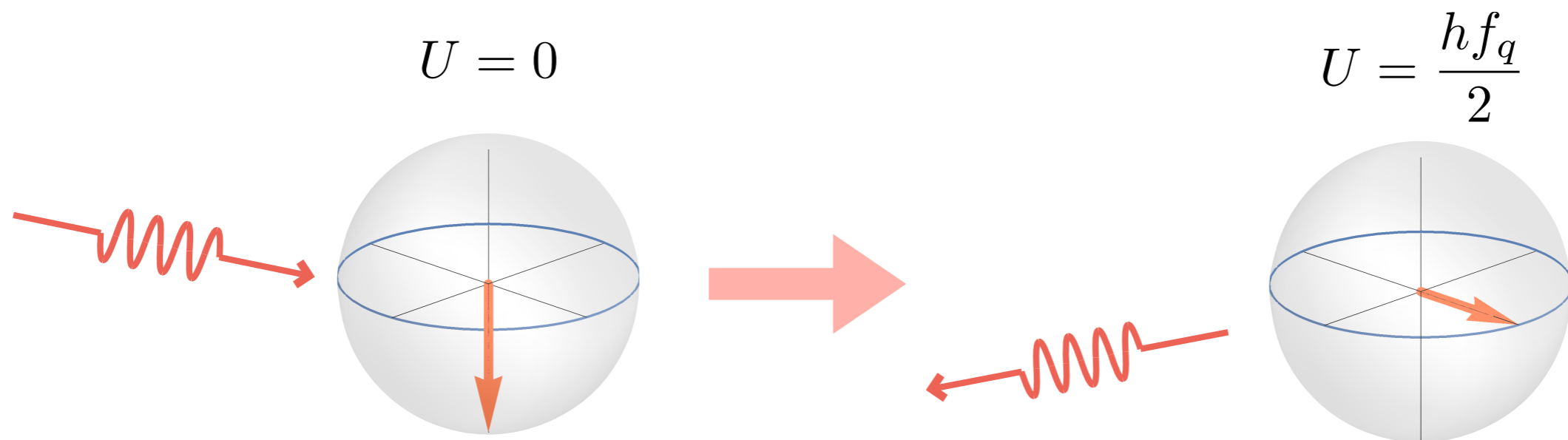
so, where does the « quantum heat » comes from?

# Thermodynamics of preparing a quantum superposition





# Thermodynamics of preparing a quantum superposition



more accurate description

$$|\alpha\rangle \otimes |g\rangle$$

$$\frac{|\psi_g\rangle \otimes |g\rangle + |\psi_e\rangle \otimes |e\rangle}{\sqrt{2}}$$

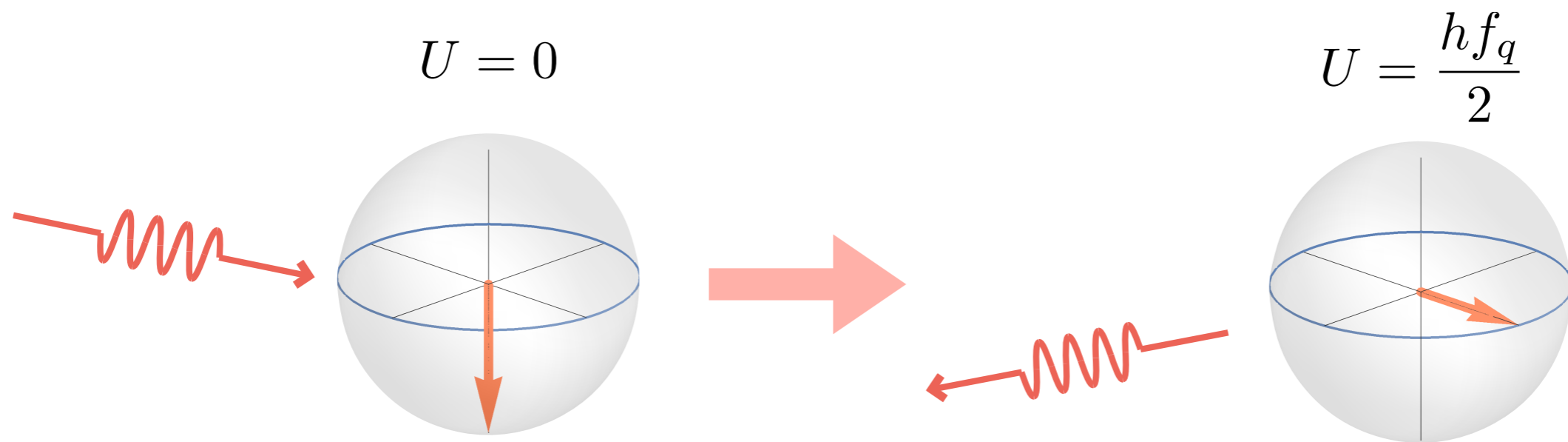
where  $\langle a^\dagger a \rangle_{|\psi_g\rangle} = 1 + \langle a^\dagger a \rangle_{|\psi_e\rangle}$

superposition of two cases

field did not give a quantum of work to system + it did

$$\frac{|\psi_g\rangle \otimes |g\rangle + |\psi_e\rangle \otimes |e\rangle}{\sqrt{2}}$$

# Thermodynamics of preparing a quantum superposition



more accurate description

$$|\alpha\rangle \otimes |g\rangle$$

$$\frac{|\psi_g\rangle \otimes |g\rangle + |\psi_e\rangle \otimes |e\rangle}{\sqrt{2}}$$

where  $\langle a^\dagger a \rangle_{|\psi_g\rangle} = 1 + \langle a^\dagger a \rangle_{|\psi_e\rangle}$

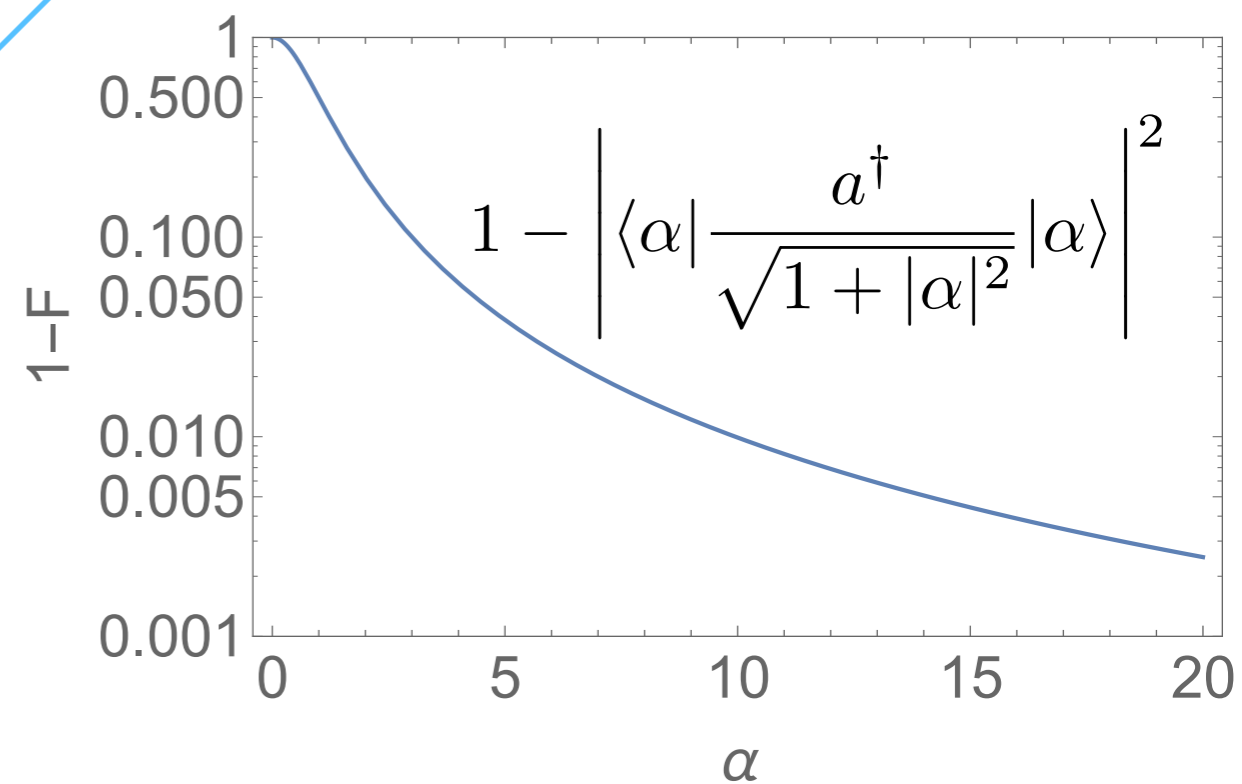
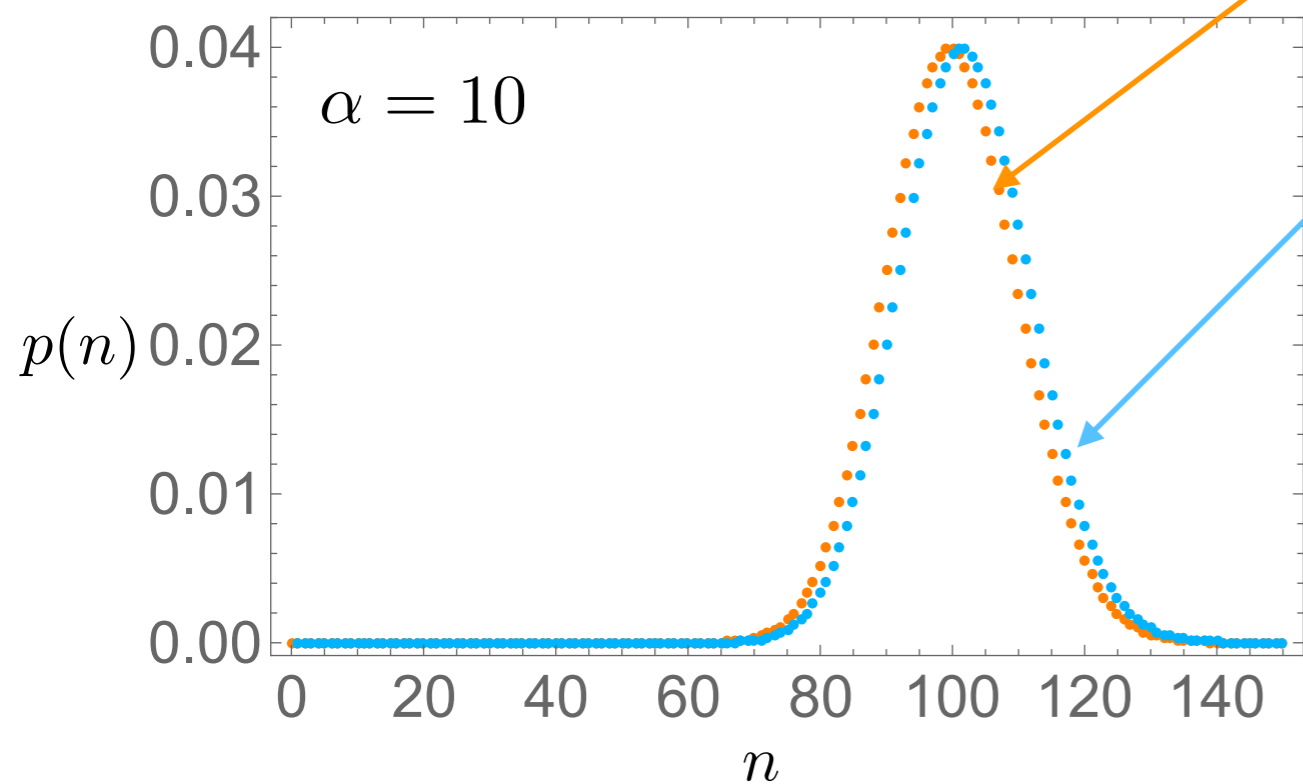
note that the qubit-field interaction barely modifies the field state if  $\alpha \gg 1$

$\langle \psi_g | \psi_e \rangle \rightarrow 1$  does not prevent  $\langle \psi_g | a^\dagger a | \psi_g \rangle - \langle \psi_e | a^\dagger a | \psi_e \rangle = 1$

$\alpha \gg 1 \Rightarrow \frac{|\psi_g\rangle \otimes |g\rangle + |\psi_e\rangle \otimes |e\rangle}{\sqrt{2}} \approx |\alpha\rangle \otimes \frac{|g\rangle + |e\rangle}{\sqrt{2}}$  **almost zero correlations**  
**yet, a measurable energy difference!**

# can one measure it in single shot?

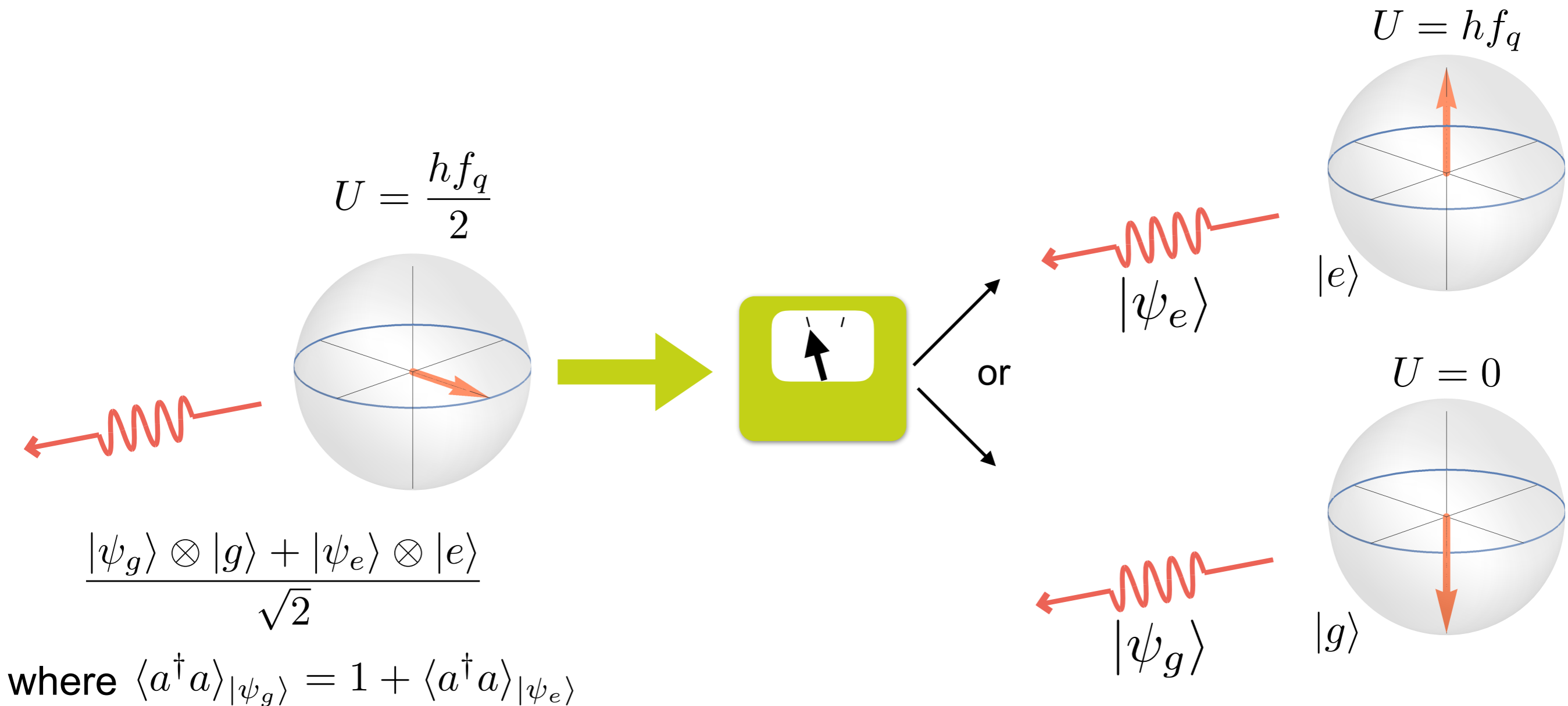
simple example:  $|\alpha\rangle$  and  $\frac{a^\dagger|\alpha\rangle}{\sqrt{1+|\alpha|^2}}$



in one shot, no measurement can tell with high fidelity whether one state of the other

**energy difference can be measured on average only**

# where does the « quantum heat » comes from?

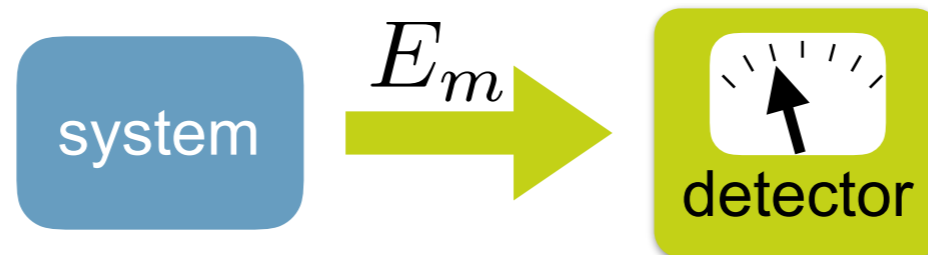


measurement **reveals** what amount of **work** has been transferred from the drive to the qubit

**can we measure this energy difference in the drive?**

# « quantum heat »

« quantum heat »



**does it obey a second law?**

**yes**, fluctuation theorems can be extended with this work and « heat »

**can it fuel an engine?**

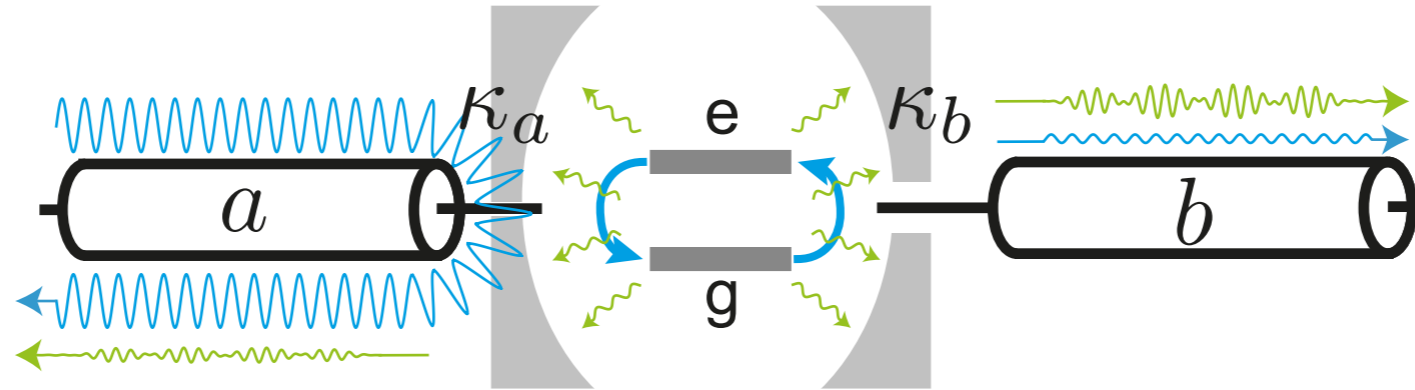
**yes**, repeatedly measuring  $\sigma_x$  on a qubit can provide work on a cycle

**what provides this energy?**

the **work** used to prepare the system state

**can it be measured directly and not just inferred?**

# What do the output lines contain?



input-output theory

+

adiabatic elimination of the cavity

$$\langle a_{out} \rangle = \langle a_{out} \rangle_0 - \sqrt{\gamma_a} \langle \sigma_- \rangle_{\rho(t)}$$

reflected  
driving field

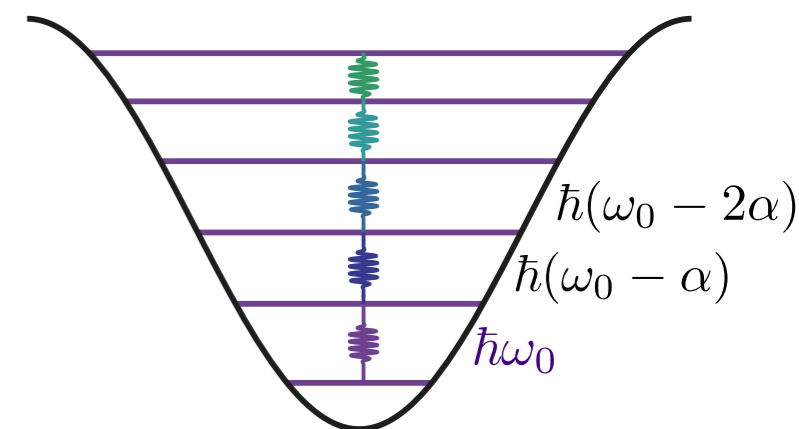
$$\frac{\gamma_a}{\gamma_b} = \frac{\kappa_a}{\kappa_b} \ll 1$$

$$\gamma_i = \kappa_i \frac{\chi}{2\alpha}$$

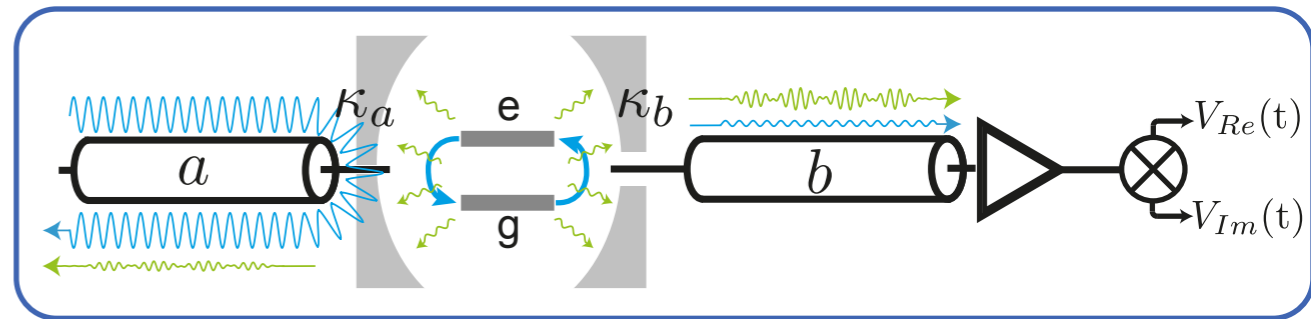
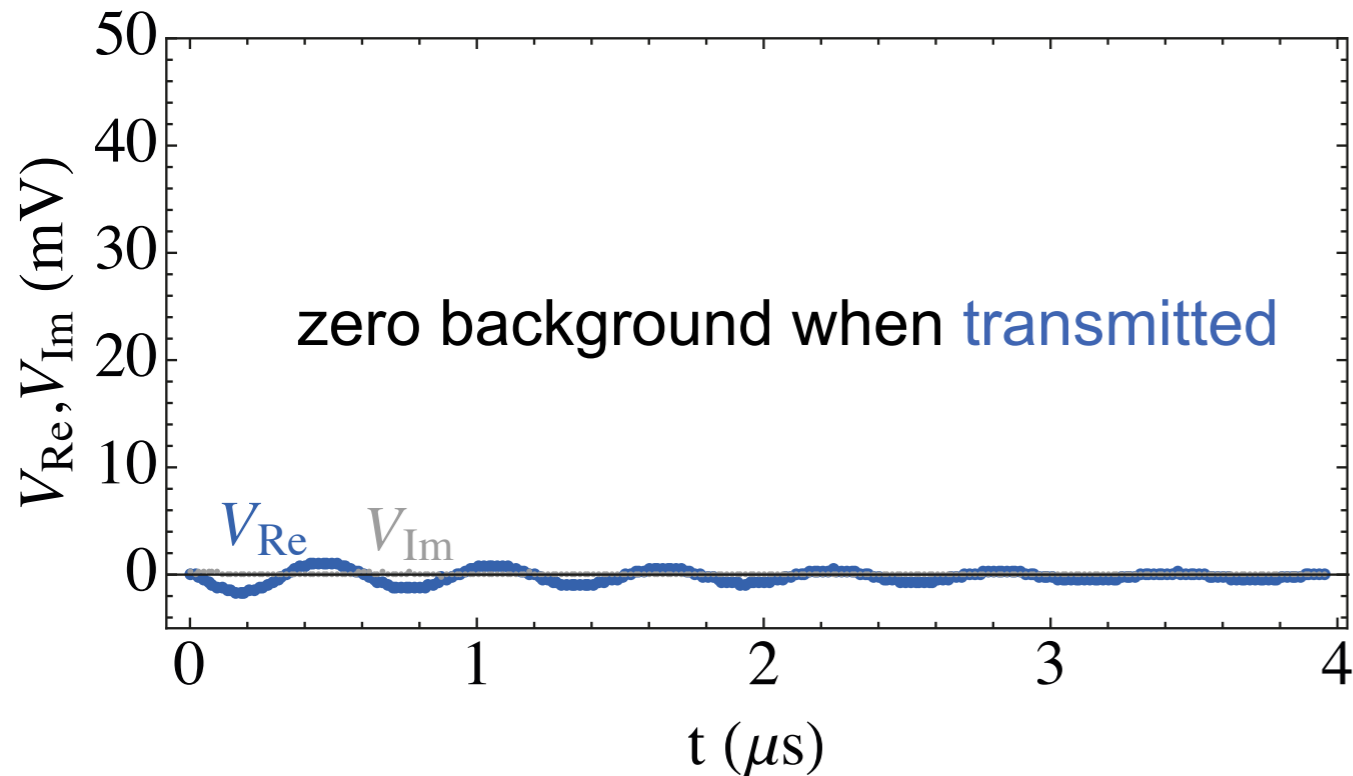
$$\langle b_{out} \rangle = \langle b_{out} \rangle_0 - \sqrt{\gamma_b} \langle \sigma_- \rangle_{\rho(t)}$$

transmitted  
driving field

$$H_{\text{coupl}} = -\hbar \chi a^\dagger a |e\rangle \langle e|$$

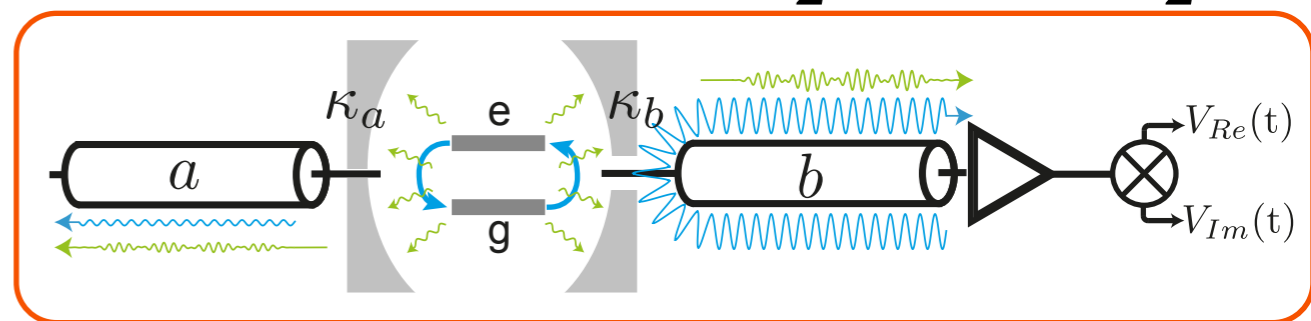
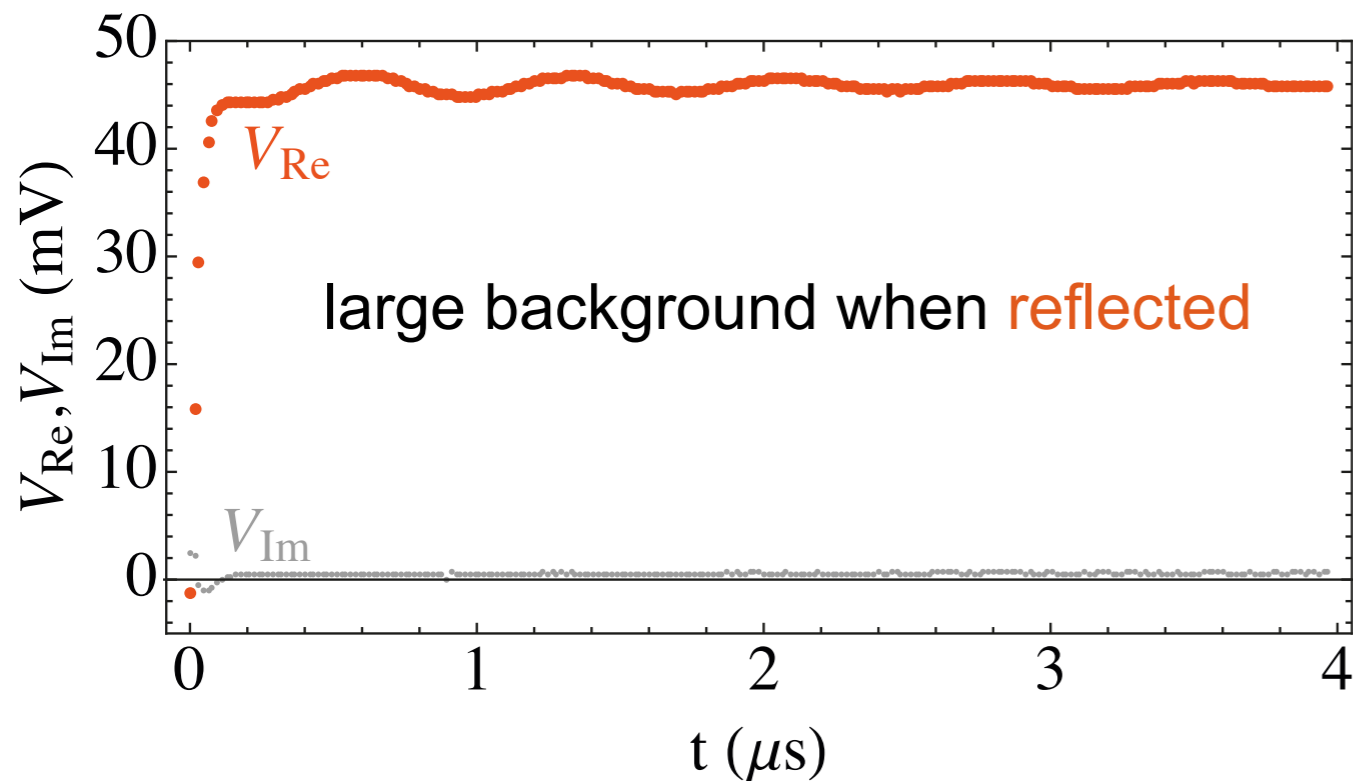


# Amplitude of fluorescence



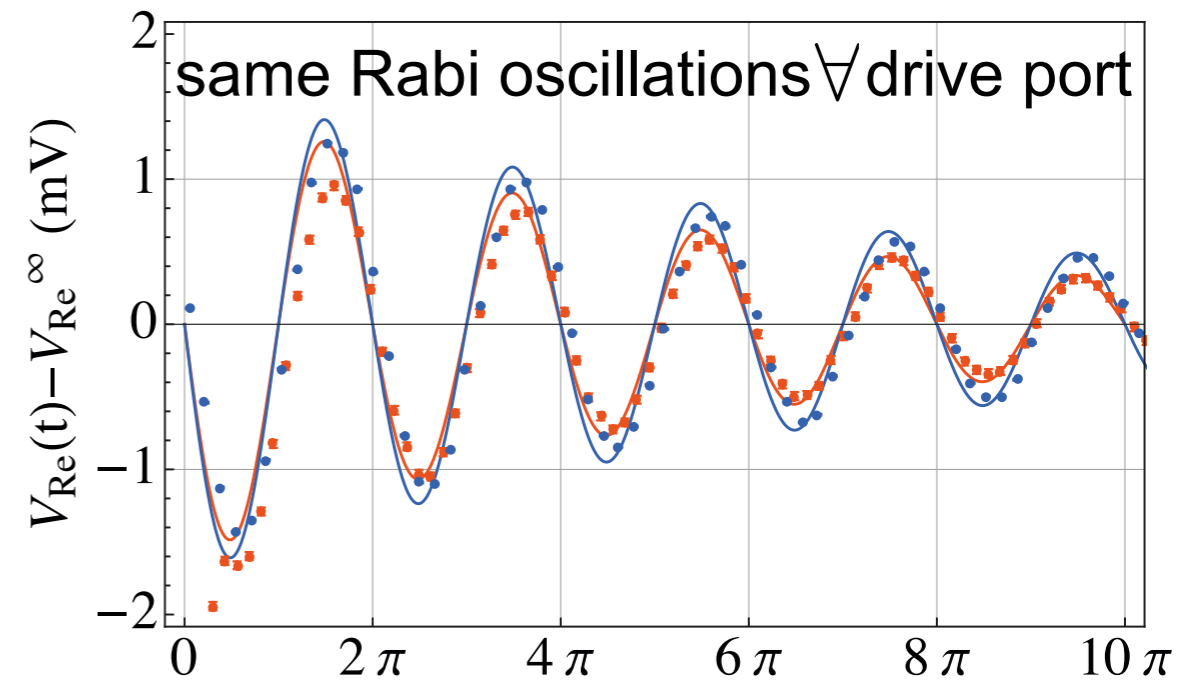
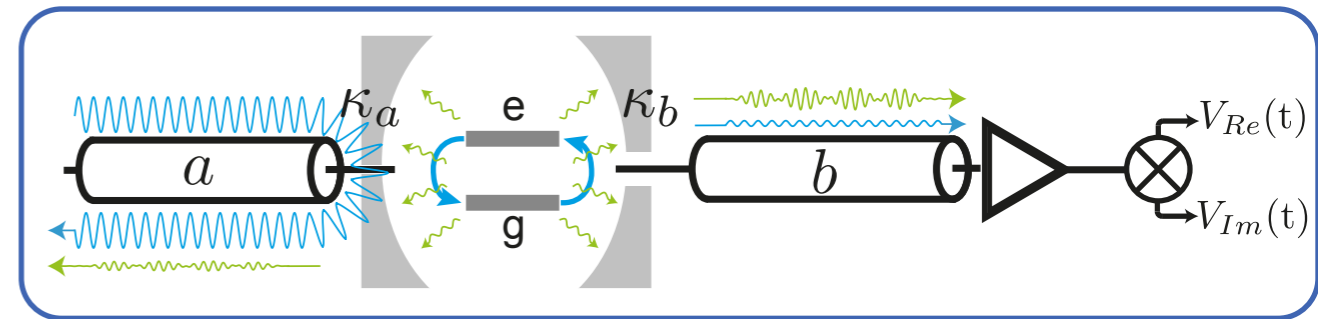
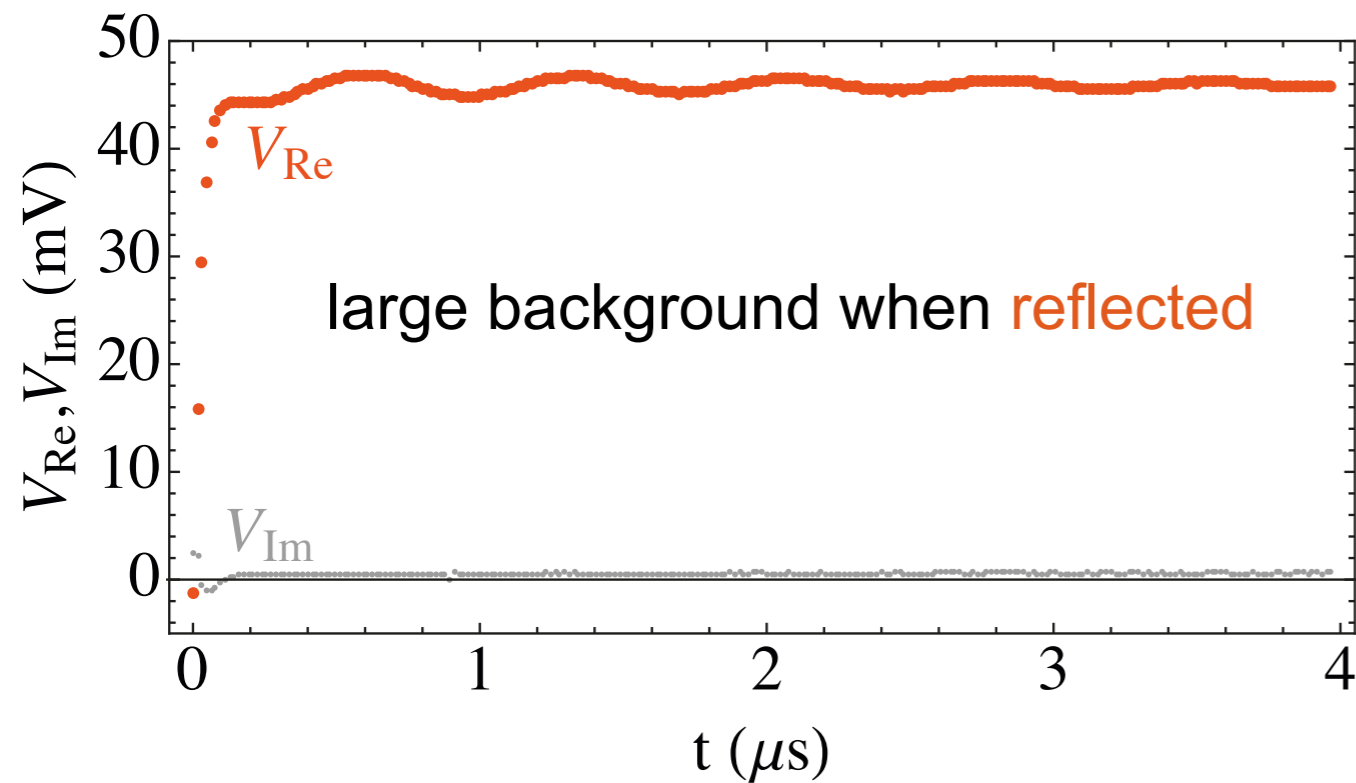
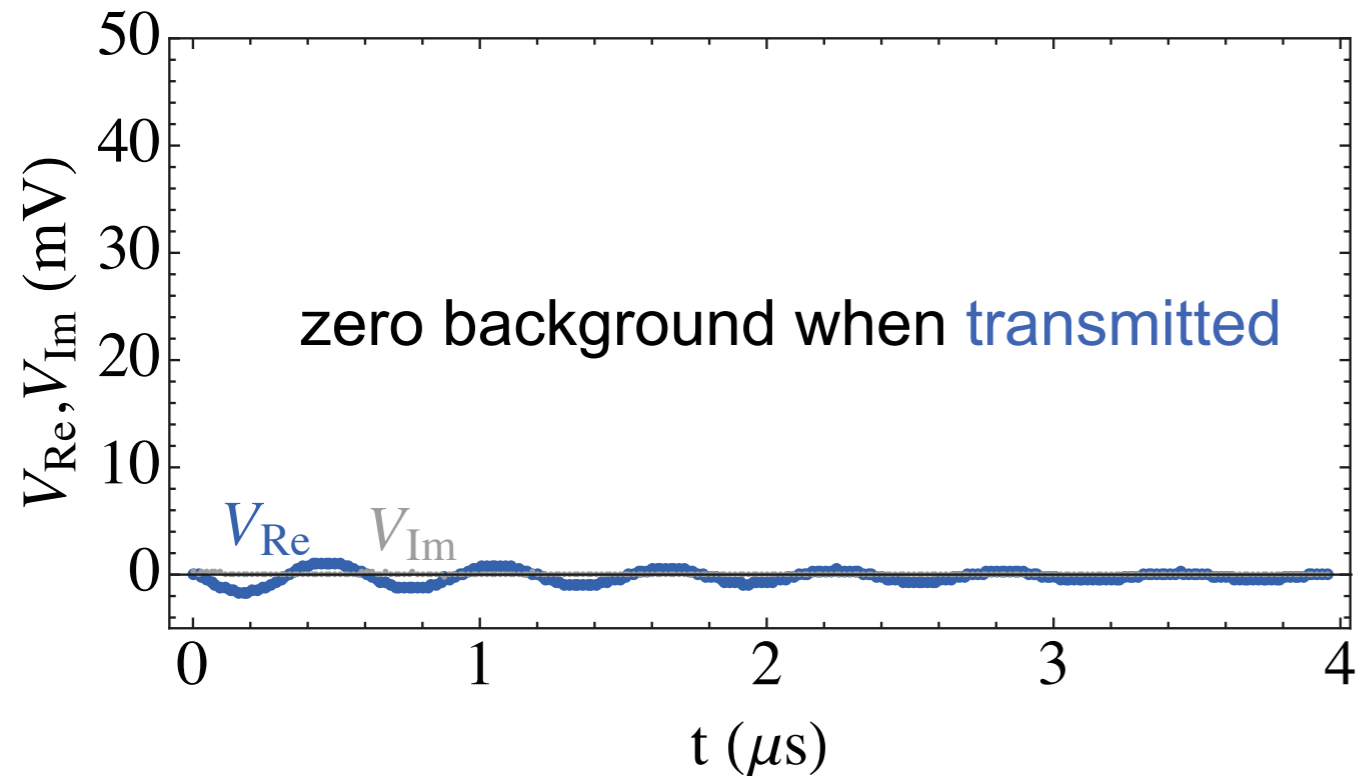
$$\langle b_{out} \rangle \propto \overline{V_{Re}} + i\overline{V_{Im}}$$

$$\langle b_{out} \rangle = \langle b_{out} \rangle_0 - \sqrt{\gamma_b} \langle \sigma_- \rangle_{\rho(t)}$$

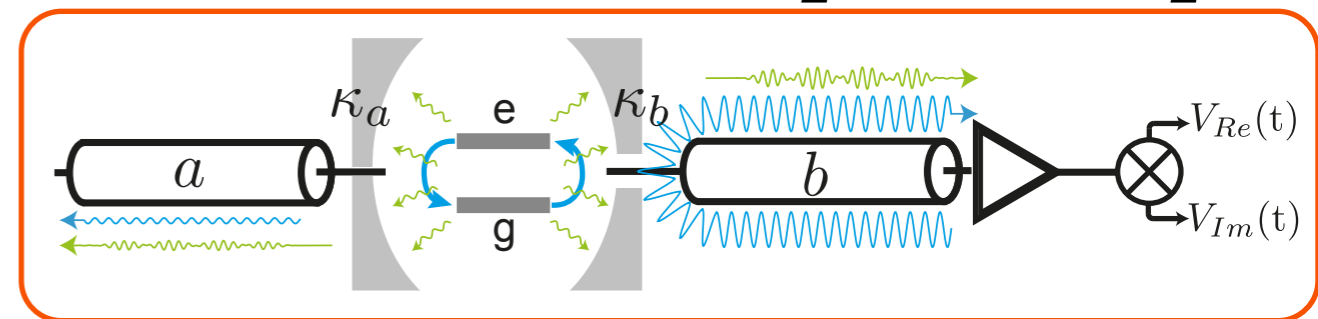


$$\langle b_{out} \rangle = \langle b_{out} \rangle_0 - \sqrt{\gamma_b} \frac{\langle \sigma_x \rangle}{2} - i\sqrt{\gamma_b} \frac{\langle \sigma_y \rangle}{2}$$

# Amplitude of fluorescence and Rabi oscillations

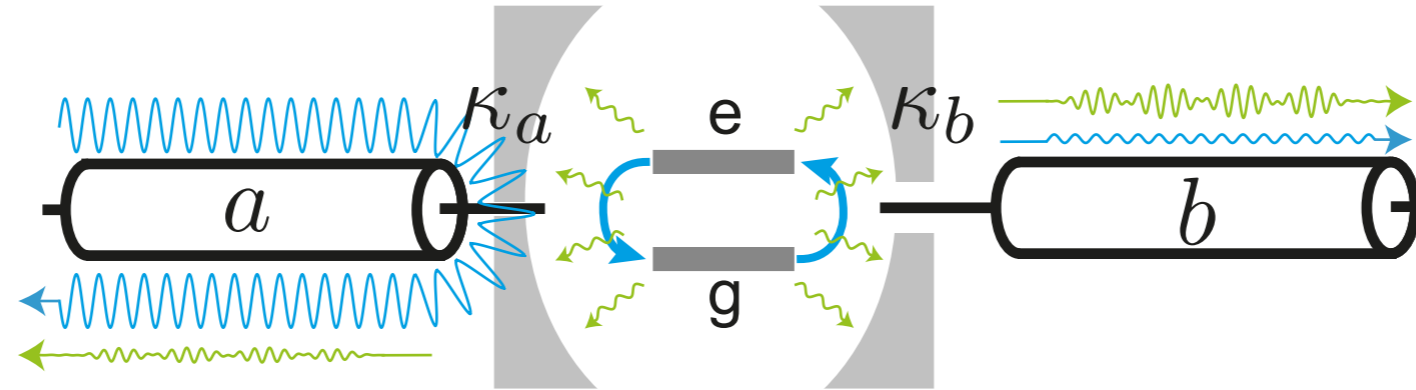


$$\langle b_{out} \rangle = \langle b_{out} \rangle_0 - \sqrt{\gamma_b} \frac{\langle \sigma_x \rangle}{2} - i \sqrt{\gamma_b} \frac{\langle \sigma_y \rangle}{2}$$





# How many photons exit into the output lines?



input-output theory

+

adiabatic elimination of the cavity

$$\langle a_{out} \rangle = \langle a_{out} \rangle_0 - \sqrt{\gamma_a} \langle \sigma_- \rangle_{\rho(t)}$$

$$\langle a_{out}^\dagger a_{out} \rangle = \langle a_{out}^\dagger a_{out} \rangle_0 + \gamma_a \frac{1 + \langle \sigma_z \rangle_{\rho(t)}}{2} + \frac{\Omega_R}{2} \langle \sigma_x \rangle_{\rho(t)}$$

spontaneous  
emission

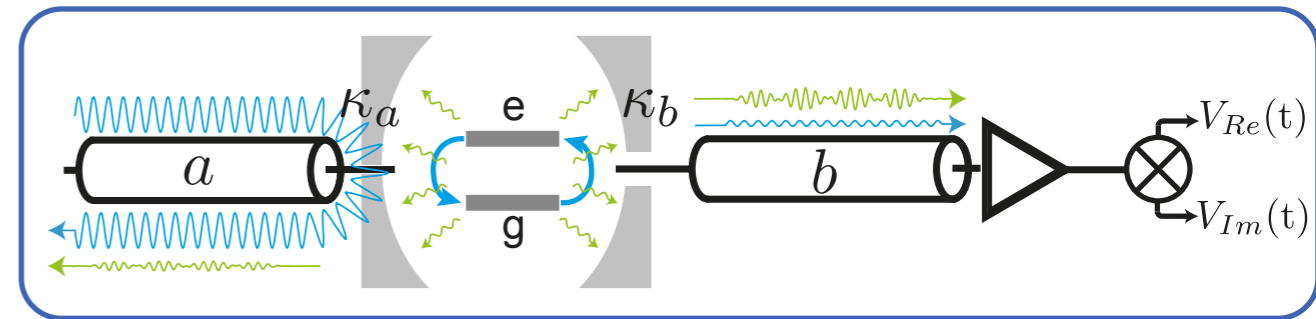
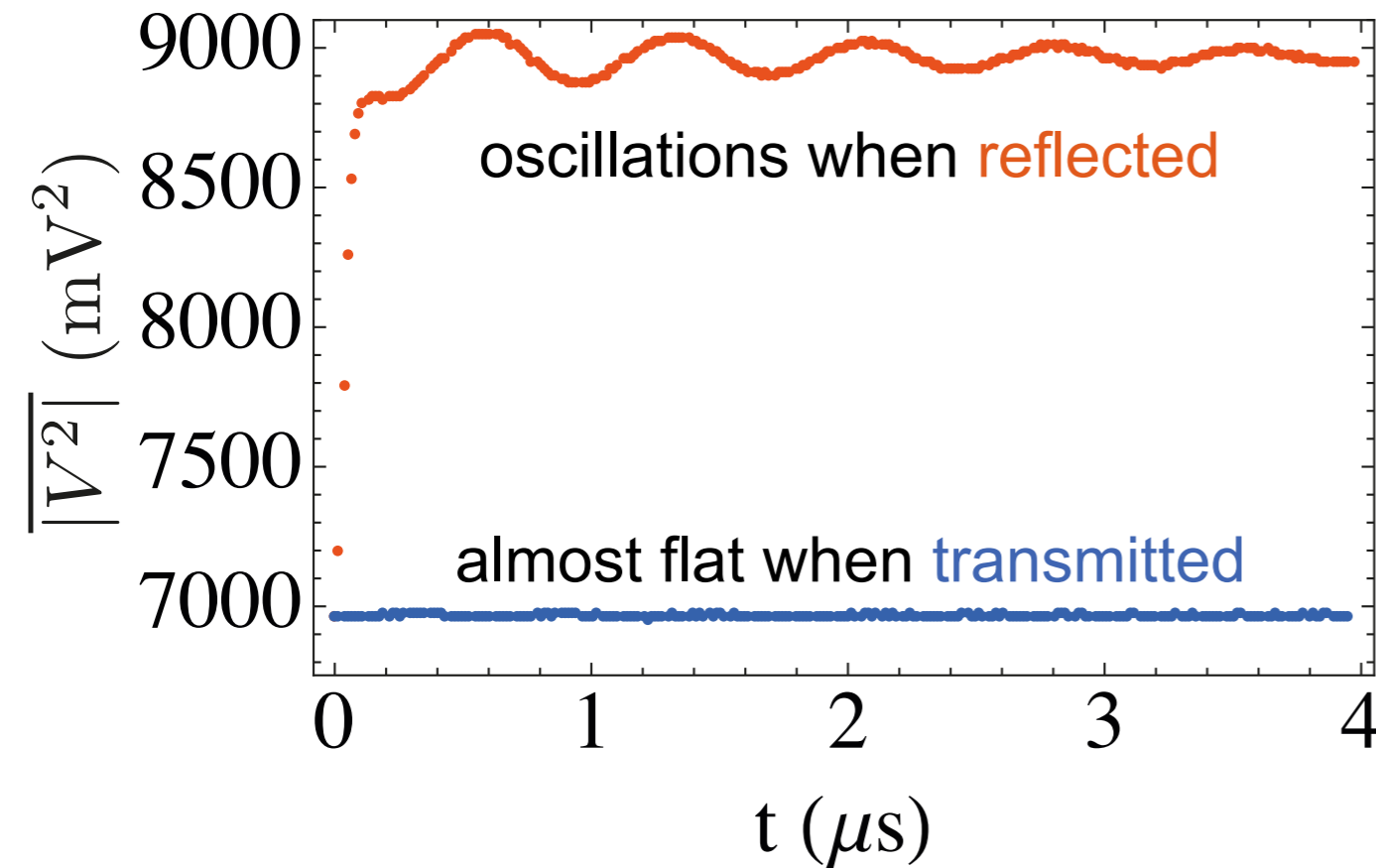
stimulated  
emission

goes back  
with reflected  
drive

$$\langle b_{out} \rangle = \langle b_{out} \rangle_0 - \sqrt{\gamma_b} \langle \sigma_- \rangle_{\rho(t)}$$

$$\langle b_{out}^\dagger b_{out} \rangle = \langle b_{out}^\dagger b_{out} \rangle_0 + \gamma_b \frac{1 + \langle \sigma_z \rangle_{\rho(t)}}{2}$$

# How many photons exit into the output lines?



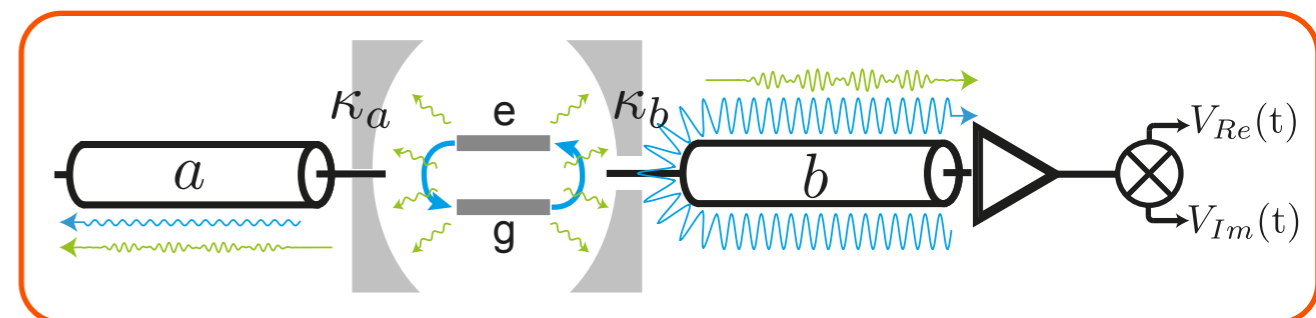
$$\langle b_{out} \rangle \propto \overline{V_{Re}} + i \overline{V_{Im}}$$

$$\langle b_{out}^\dagger b_{out} \rangle \propto \overline{|V|^2} = \overline{V_{Re}^2} + \overline{V_{Im}^2}$$

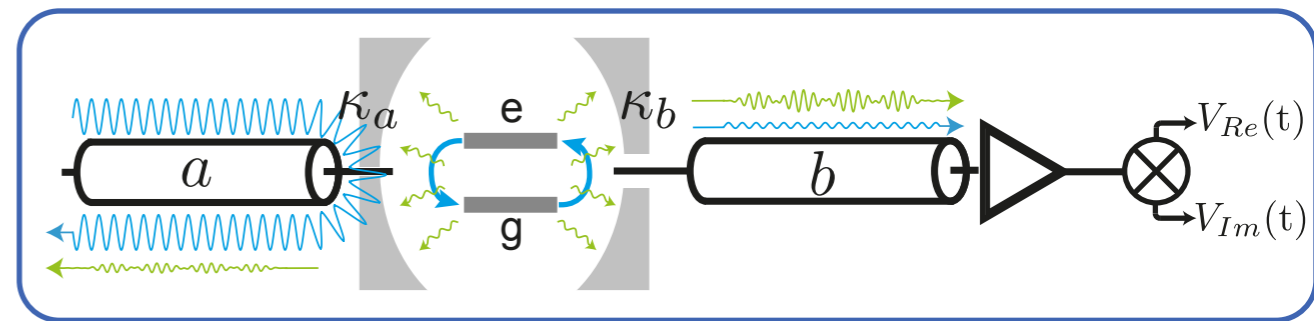
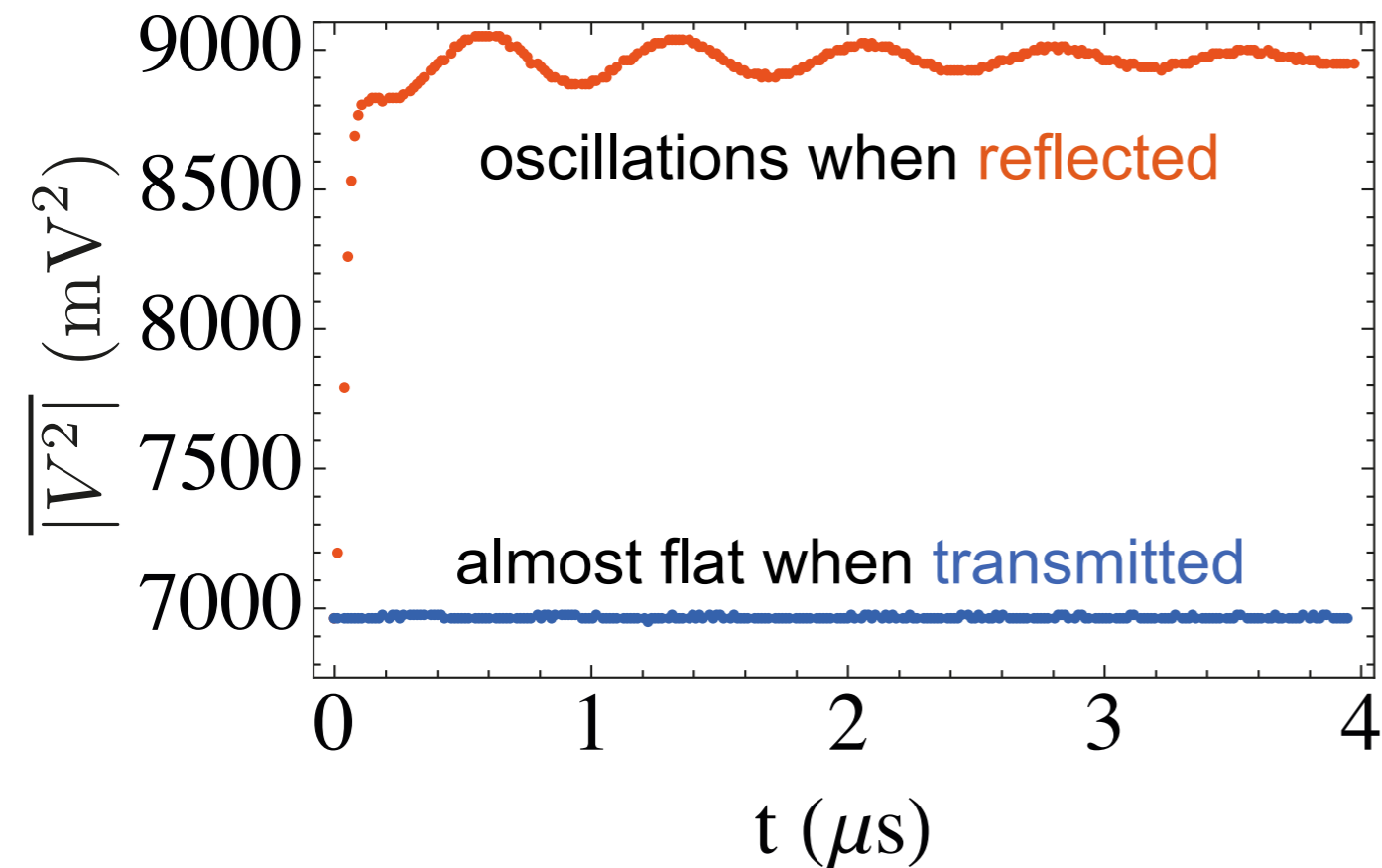
$$\langle b_{out}^\dagger b_{out} \rangle = \langle b_{out}^\dagger b_{out} \rangle_0 + \gamma_b \frac{1 + \langle \sigma_z \rangle_{\rho(t)}}{2}$$

$$+ \frac{\Omega_R}{2} \langle \sigma_x \rangle_{\rho(t)}$$

$$\gamma_b \approx (2 \mu\text{s})^{-1} \ll \frac{\Omega_R}{2} \approx (0.2 \mu\text{s})^{-1}$$



# How many photons exit into the output lines?



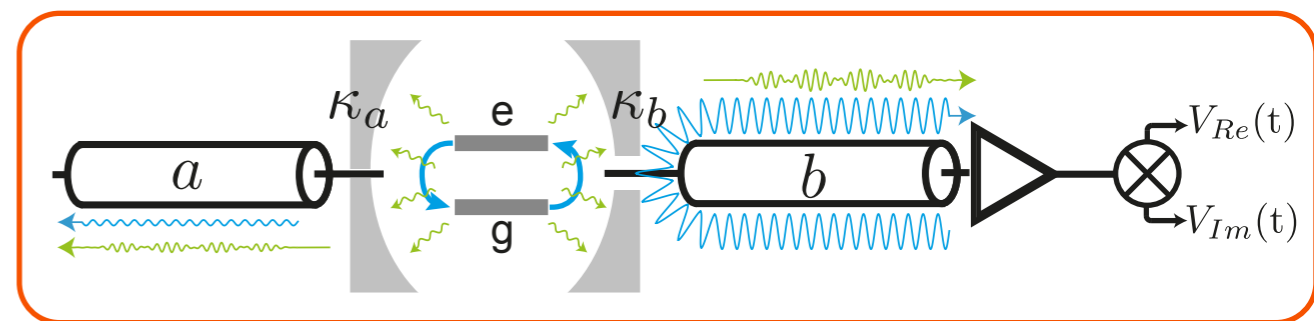
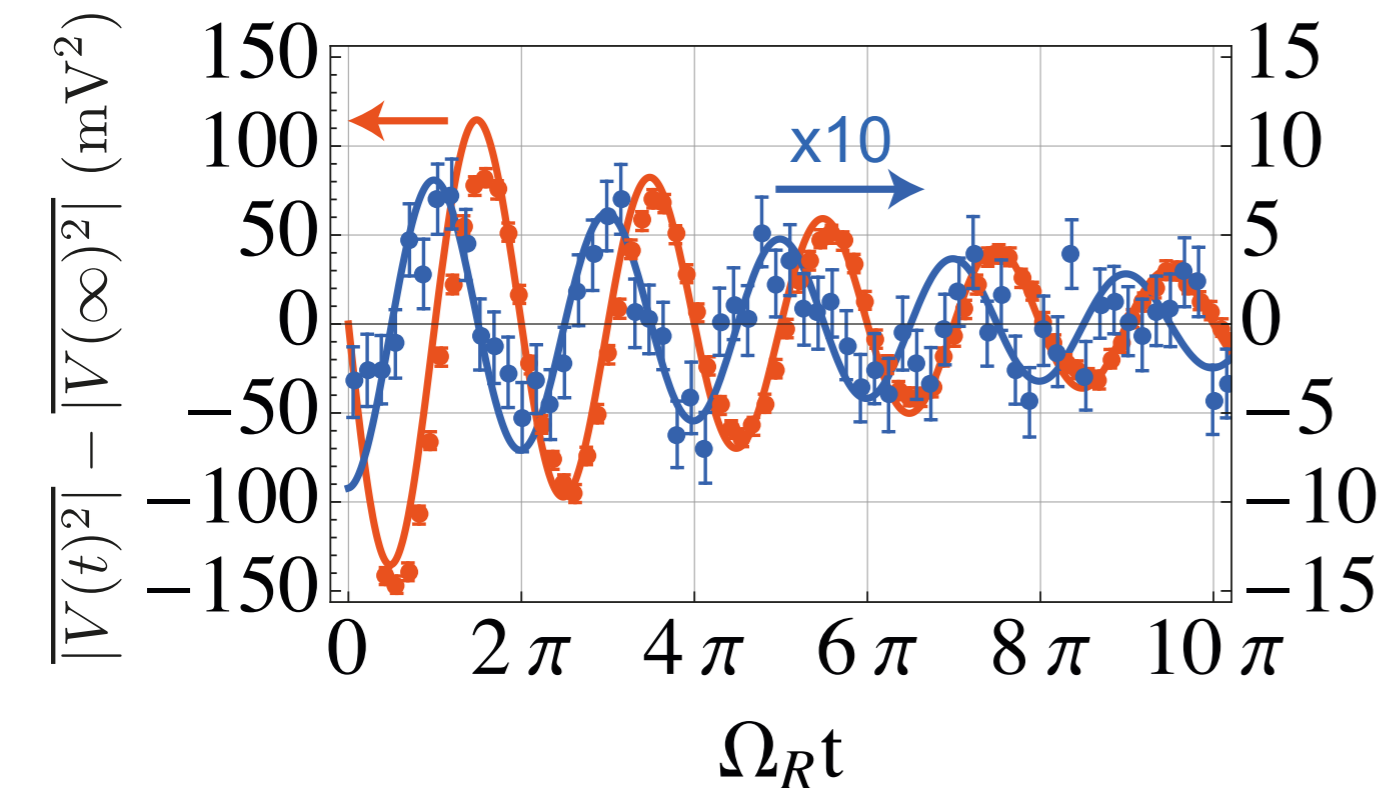
$$\langle b_{out} \rangle \propto \overline{V_{Re}} + i \overline{V_{Im}}$$

$$\langle b_{out}^\dagger b_{out} \rangle \propto \overline{|V|^2} = \overline{V_{Re}^2} + \overline{V_{Im}^2}$$

$$\langle b_{out}^\dagger b_{out} \rangle = \langle b_{out}^\dagger b_{out} \rangle_0 + \gamma_b \frac{1 + \langle \sigma_z \rangle_{\rho(t)}}{2}$$

$$+ \frac{\Omega_R}{2} \langle \sigma_x \rangle_{\rho(t)}$$

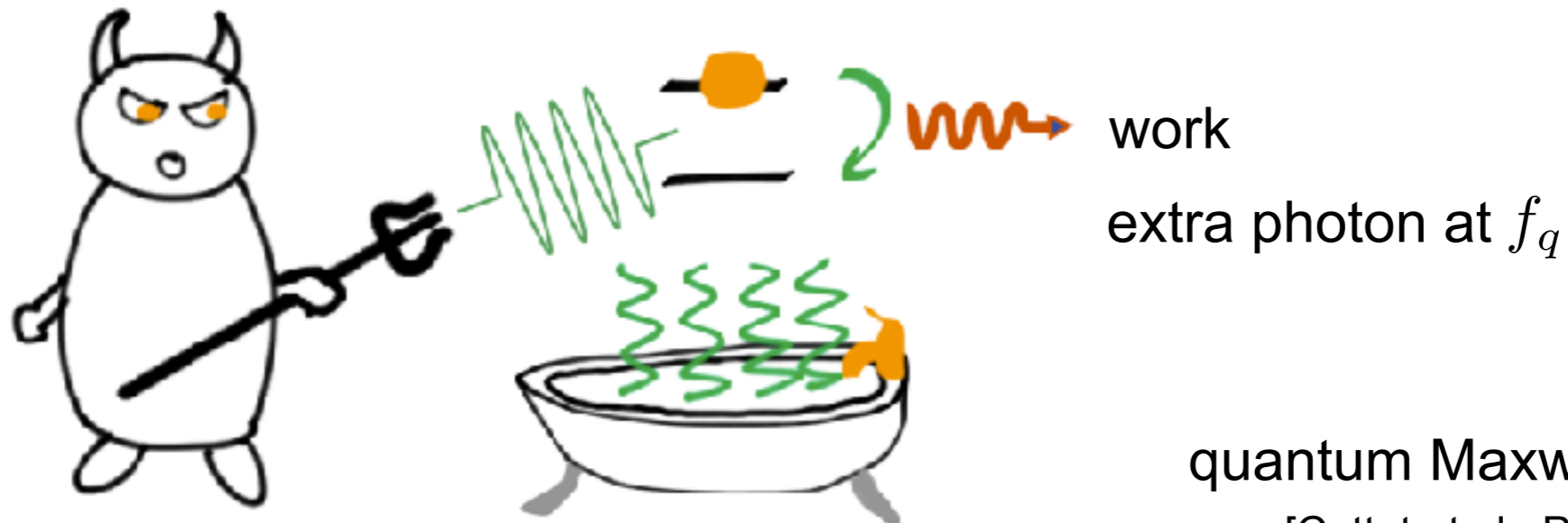
$$\gamma_b \approx (2 \mu\text{s})^{-1} \ll \frac{\Omega_R}{2} \approx (0.2 \mu\text{s})^{-1}$$



Rabi oscillations of  $\langle \sigma_z \rangle$  when **transmitted**

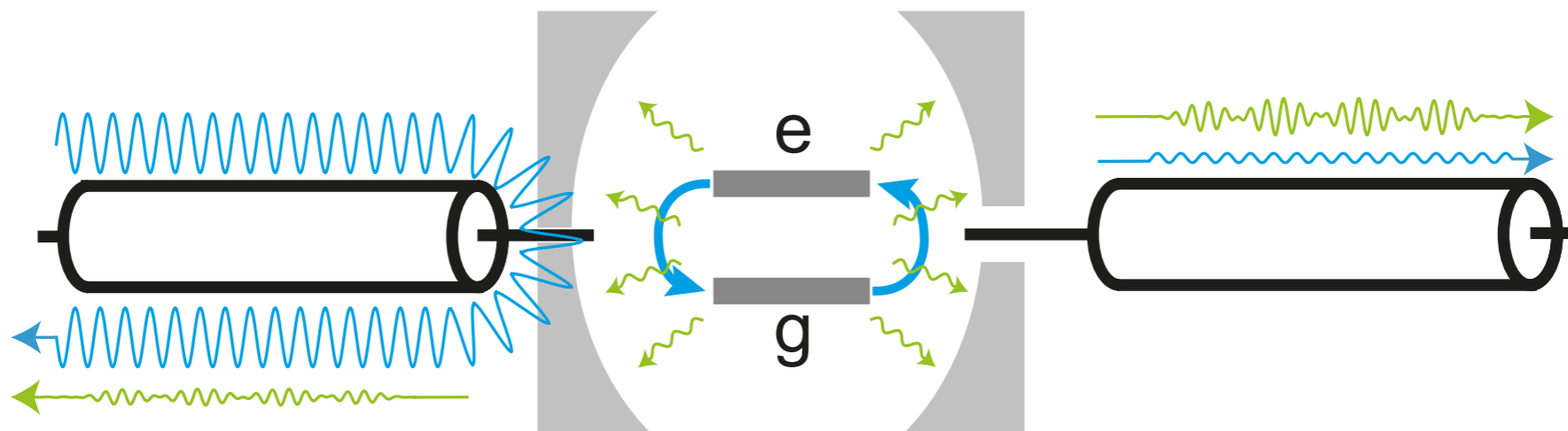
Rabi oscillations of  $\langle \sigma_x \rangle$  when **reflected**

# Measuring the outgoing energy

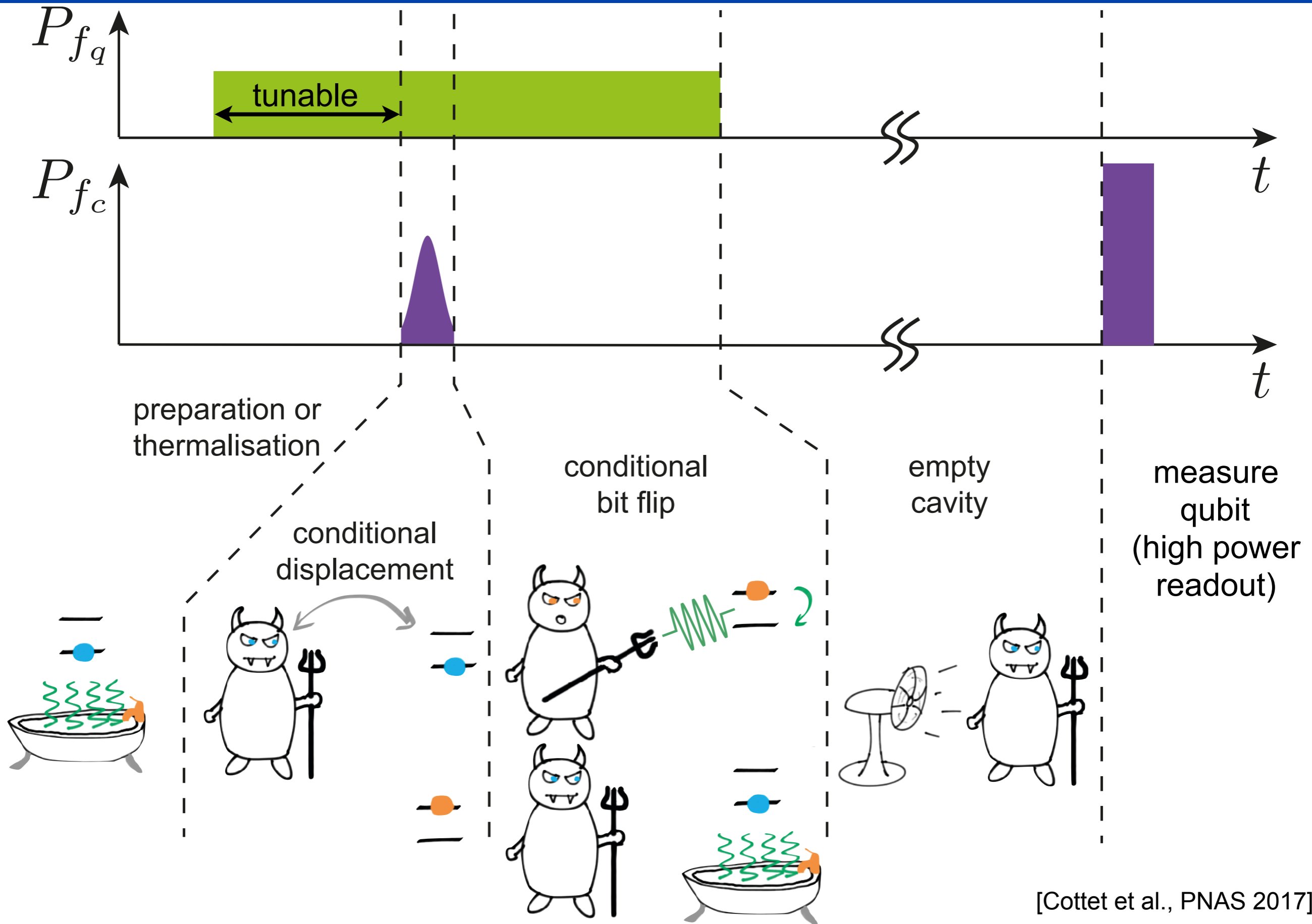


quantum Maxwell demon  
[Cottet et al., PNAS 2017]

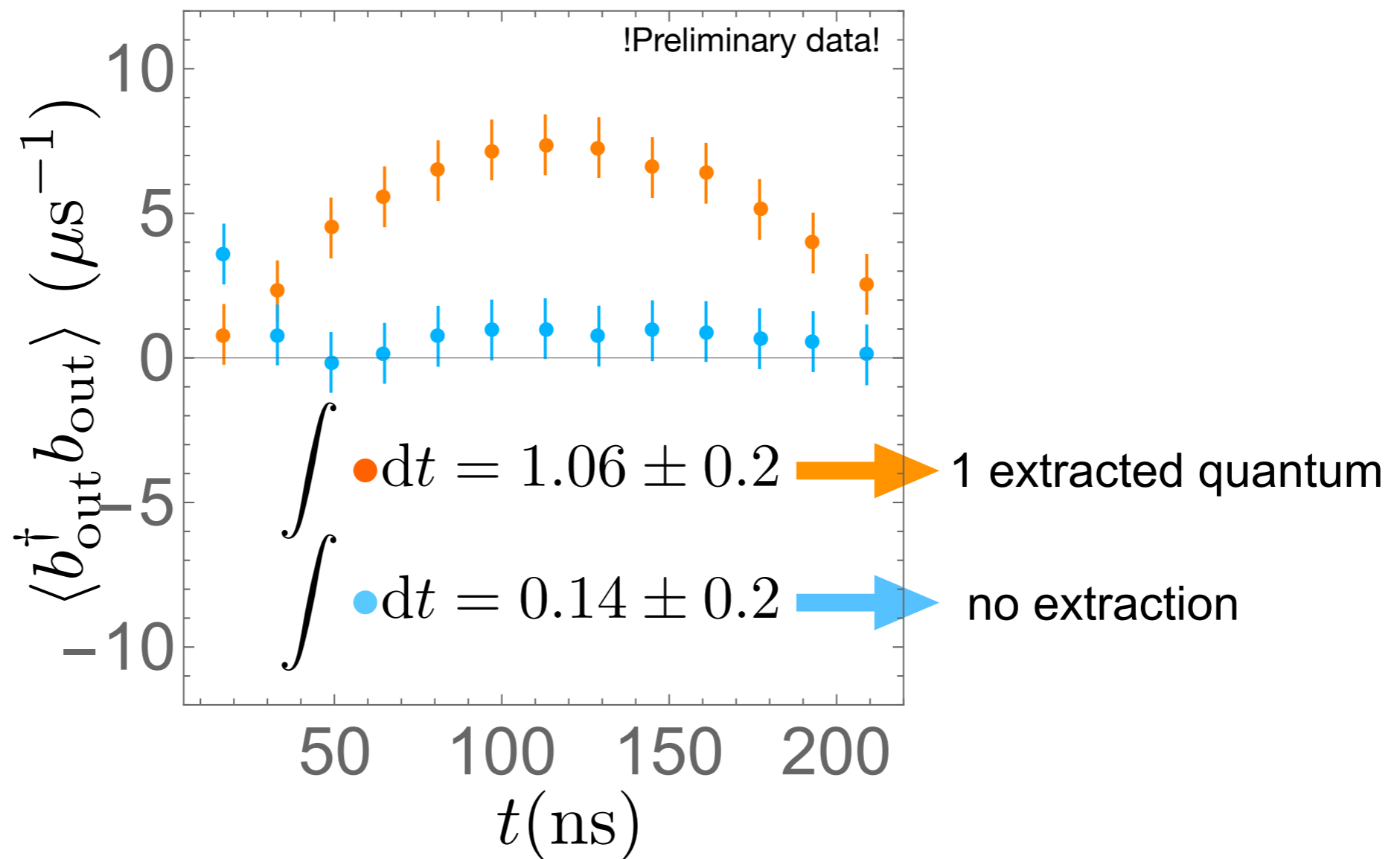
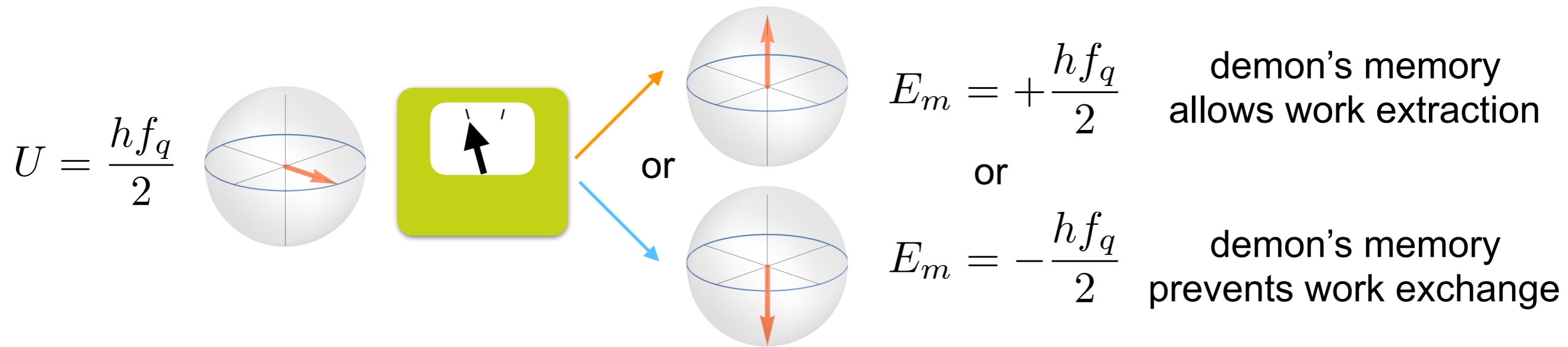
How to extract and observe a quantum of work out of a qubit?



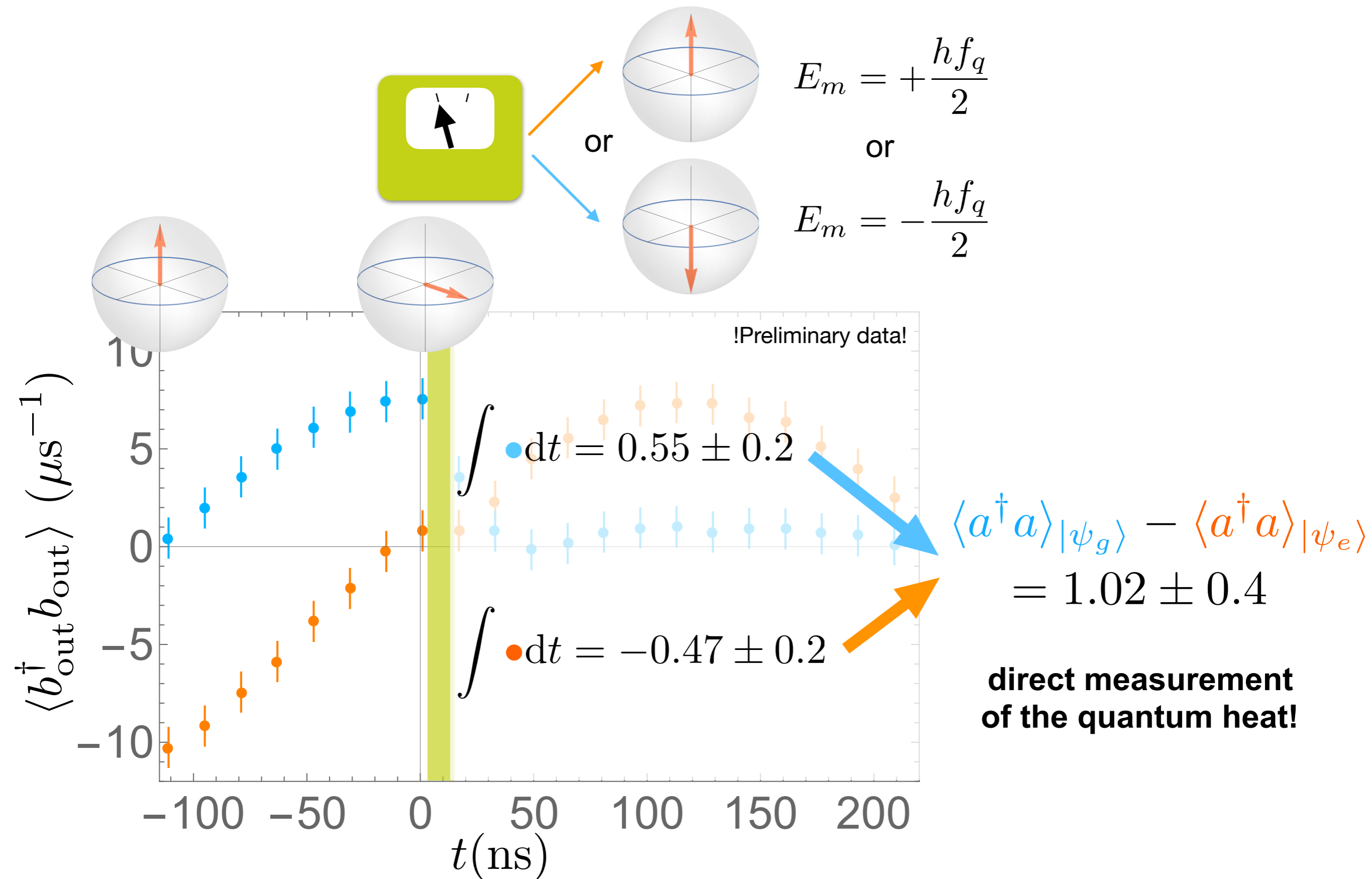
# Pulse sequence



# extracted work post selected on demon's memory

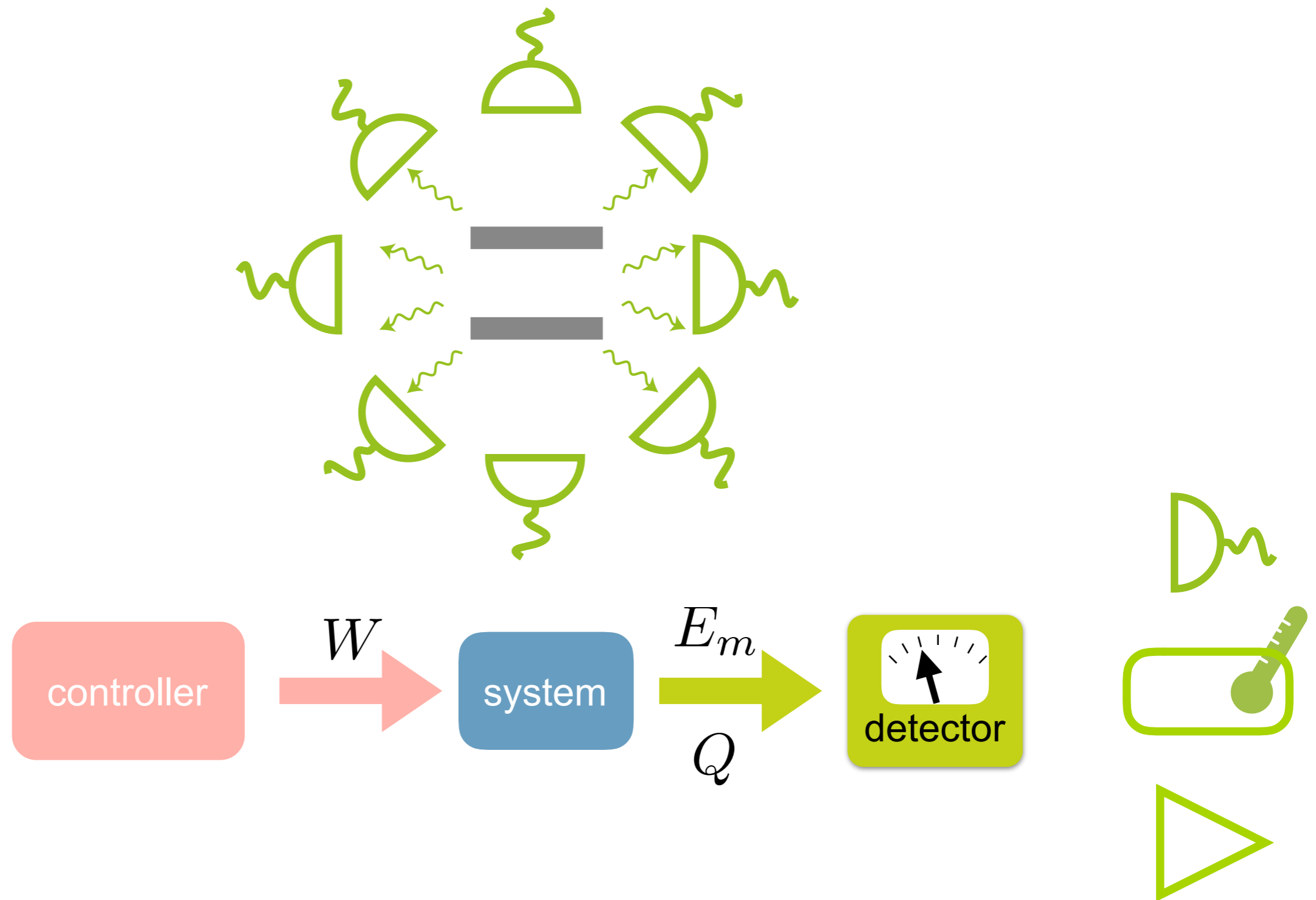


# measuring the « quantum heat »



but each signal are unexpected => **need to reproduce**

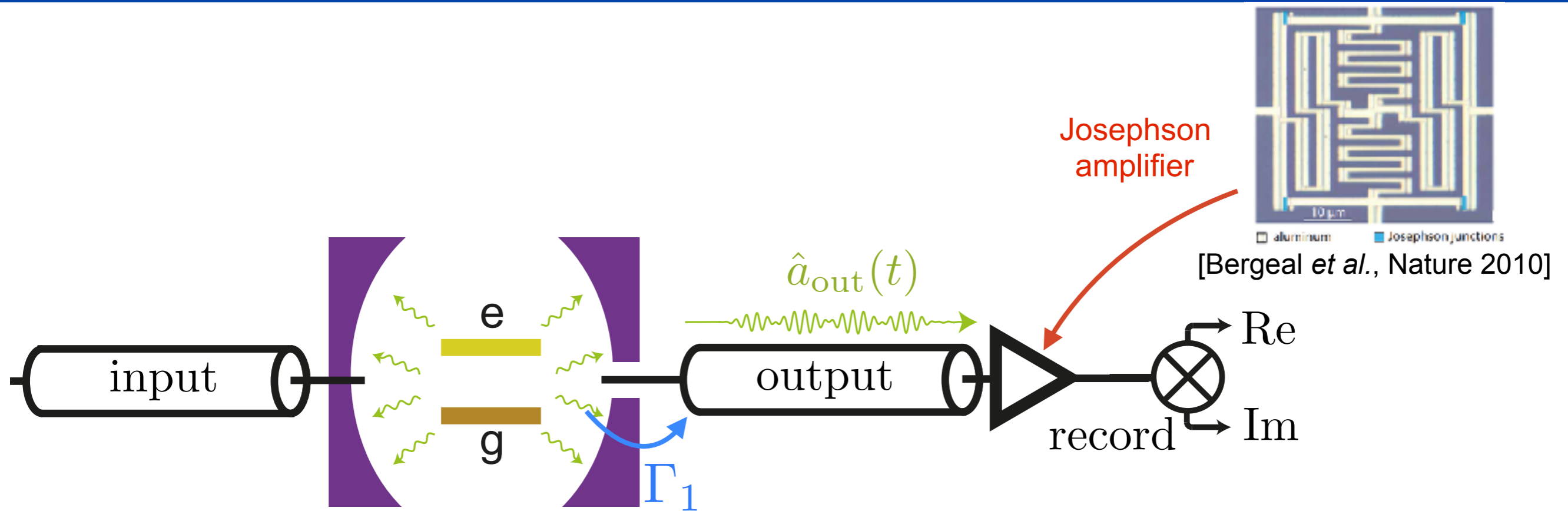
# Particular case of fluorescence measurement



**the detector can also get heat from system**



# Fluorescence Measurement



mean signal

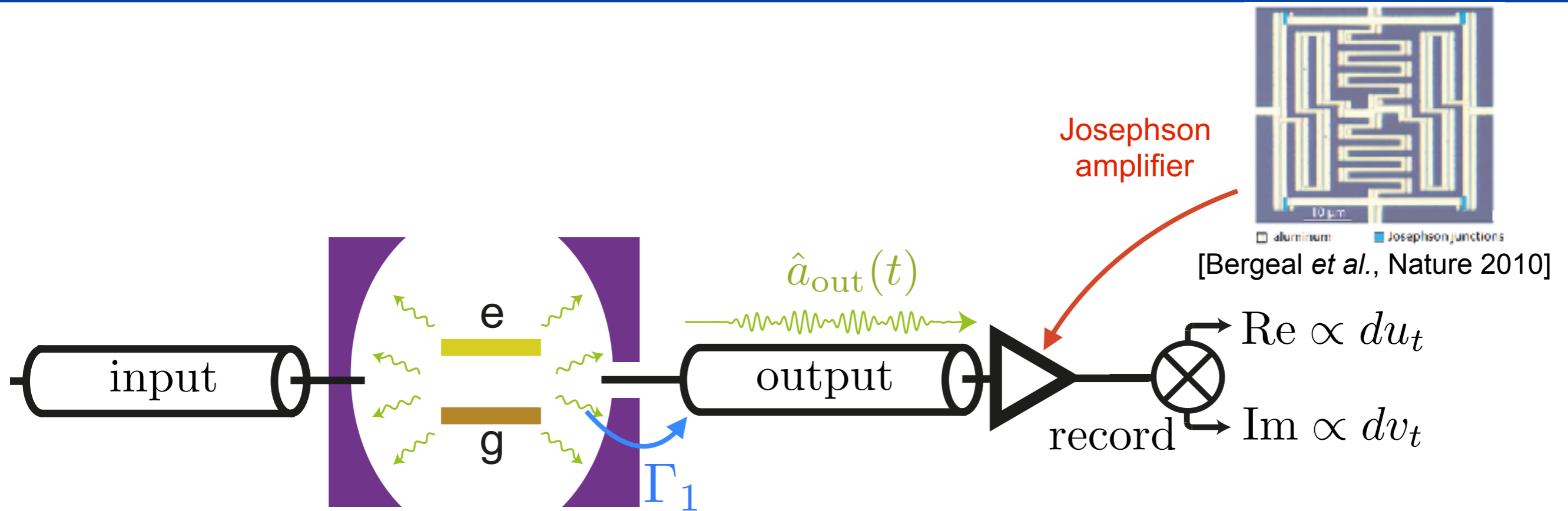
$$\langle \hat{a}_{out} \rangle \propto \sqrt{\Gamma_1} \langle \sigma_- \rangle$$



jump operator  $\propto \sigma_- = |g\rangle \langle e| = \frac{\sigma_x - i\sigma_y}{2}$

$$\Gamma_1 = (12.5 \mu\text{s})^{-1}$$

# Fluorescence Measurement



$$du_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_X \rangle_{\rho_t} dt + dW_{t,1}$$

$$dv_t = \sqrt{\frac{\eta\Gamma_1}{2}} \langle \sigma_Y \rangle_{\rho_t} dt + dW_{t,2}$$

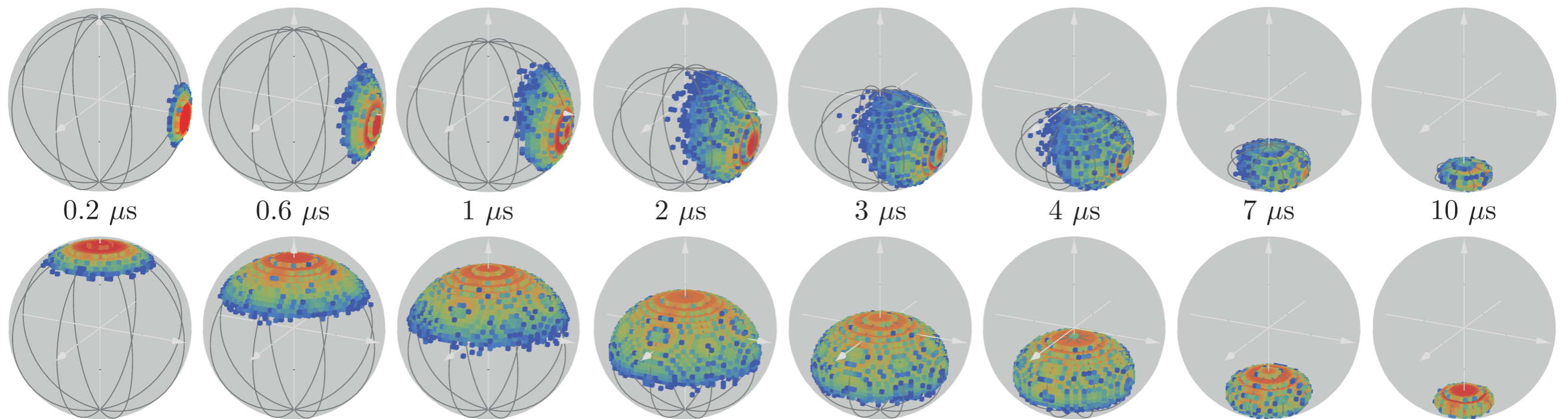
average outcome

noise (Wiener)



$\{du_t, dv_t\}$   $\xrightarrow{\text{stochastic master equation}}$   $\rho_t^B$  [Campagne-Ibarcq et al., PRX 2016]  
 [Naghiloo et al., Nat. Comm. 2016]  
 [Ficheux et al., Nat. Comm. 2017]

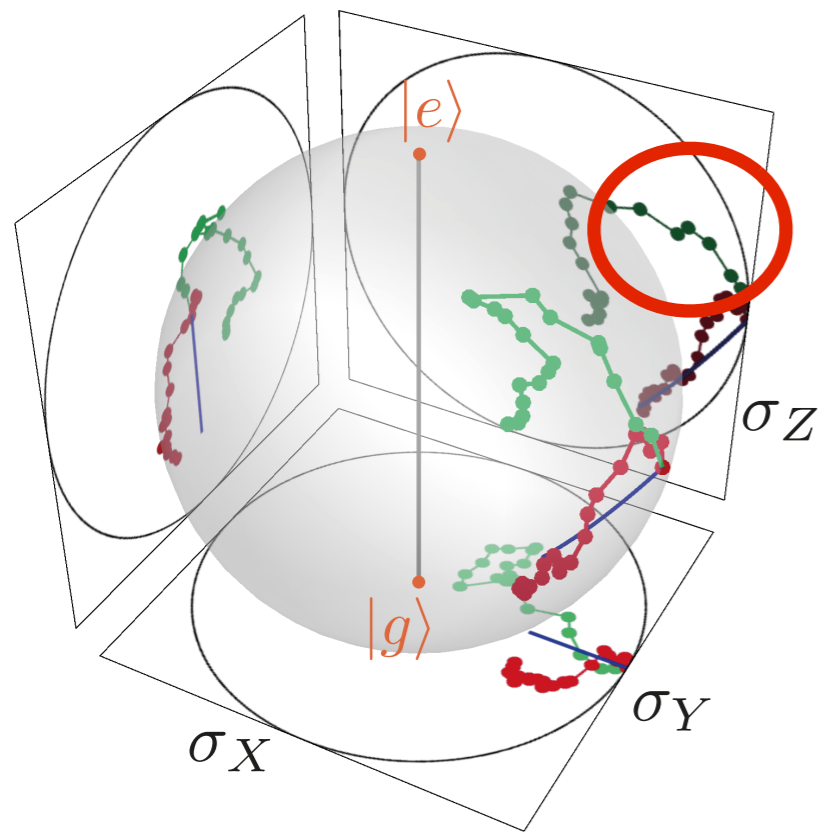
# Statistics of trajectories



[Campagne-Ibarcq *et al.*, PRX 2016]

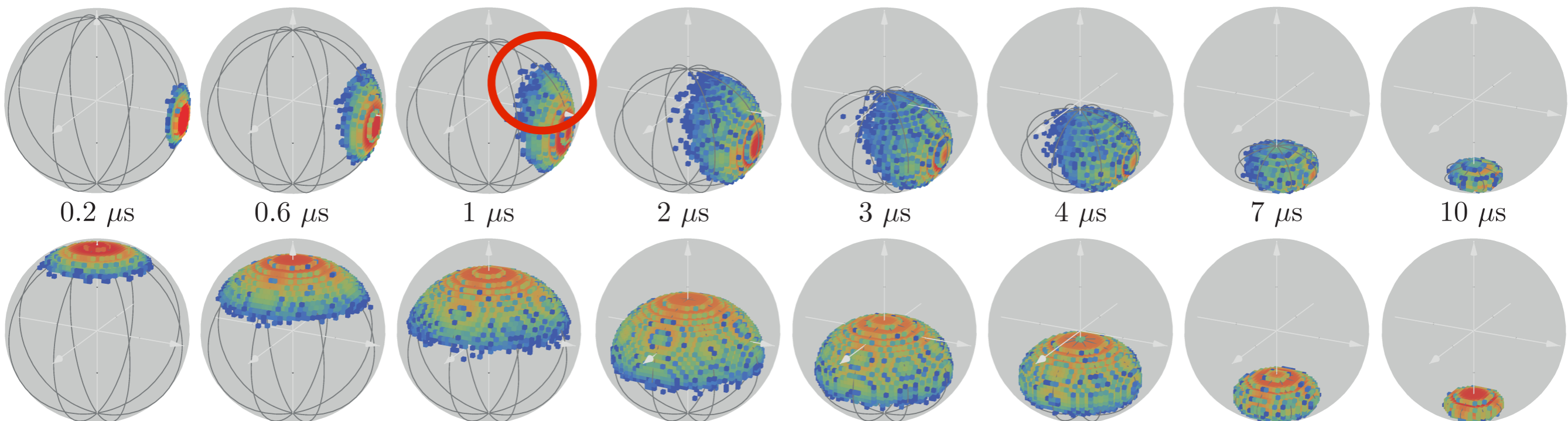
[Jordan, Chantasri, Rouchon, BH., arxiv:1511:06677]

# Counterintuitive trajectories



Energy expectation can **increase** due to the backaction of measuring spontaneously emitted photons

[Bolund and Mølmer, PRA 2014]



[Campagne-Ibarcq *et al.*, PRX 2016]

[Jordan, Chantasri, Rouchon, BH., arxiv:1511:06677]

# Conclusion

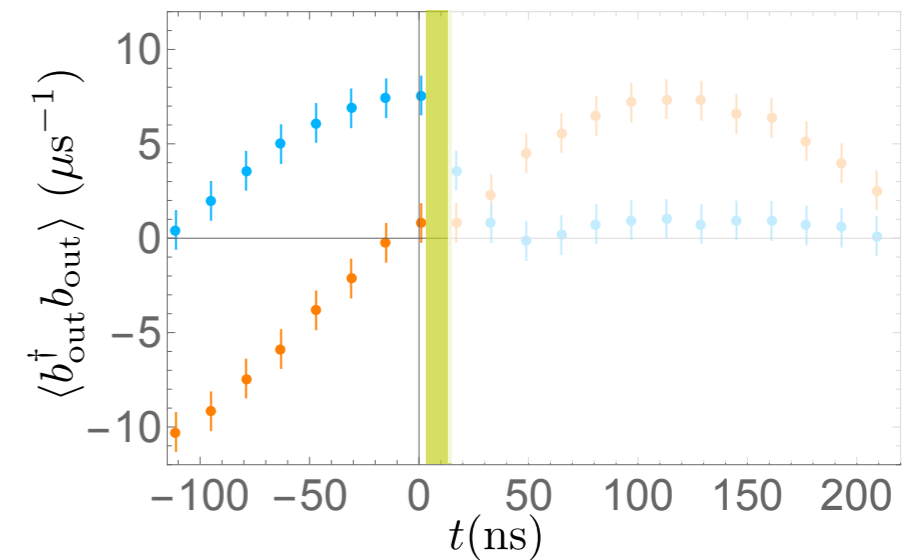
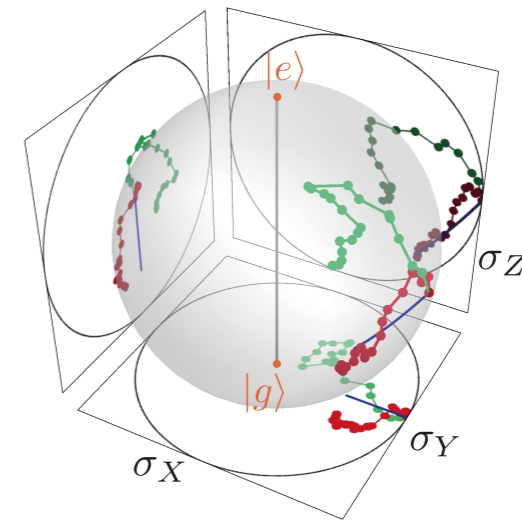
Measurement backaction leads to **changes in expected energy**

This back action energy variation (« quantum heat ») can be

- inferred from reconstructed quantum trajectory

[Campagne-Ibarcq et al., PRX 2016]  
[Ficheux et al., Nat. Comm. 2018]

- measured in the battery that prepared the system  
**on average only**



It can be used as a fuel to power up measurement based engines

[e.g. Elouard et al., PRL 2017]

# The team



Nathanaël  
Cottet



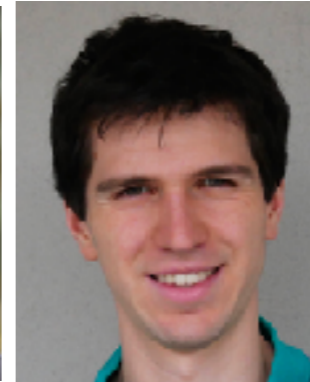
Quentin  
Ficheux



Théau  
Peronnin



Jeremy  
Stevens



Antoine  
Essig



Sébastien  
Jezouin  
(now Sherbrooke)



Philippe  
Campagne-Ibarcq  
(now Yale)



Landry  
Bretheau  
(now Polytechnique)



Pierre  
Rouchon



Mazyar  
Mirrahimi



Alain  
Sarlette



Alexia Auffèves  
(Grenoble)



Areeya  
Chantasri  
(Griffith)



Andrew  
Jordan  
(Rochester)



Cyril  
Elouard  
(Rochester)



Happy birthday Jukka!